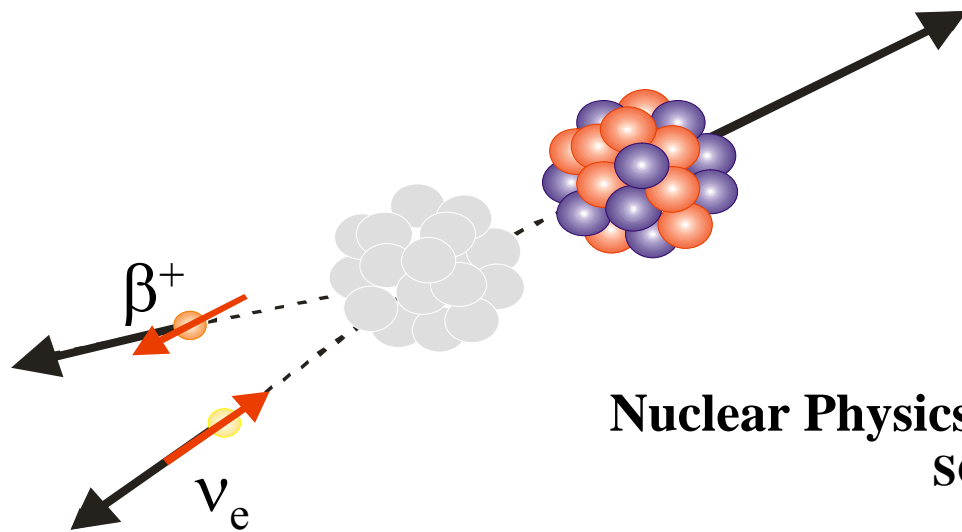


Low energy weak interaction studies using β -decay of radioactive nuclei



Nuclear Physics Research at the MYRRHA accelerator
SCK-CEN, Mol, April 06-09, 2008

Nathal Severijns
Kath. University Leuven, Belgium

Nuclei of interest

- nuclei at or close to the **$N = Z$ line**
 - nuclei with **$0^+ \rightarrow 0^+$ transitions**
 - **$T = 1/2$ mirror nuclei** ($N = Z-1 \rightarrow N = Z+1$; e.g. $^{21}\text{Na} \rightarrow ^{21}\text{Ne}$)
- nuclei with **fast** (small $\log ft$) and pure **Gamow-Teller transitions**

1. $Ft^{0^+ \rightarrow 0^+}$

- CVC
- unitarity of CKM matrix
- right-handed currents
- scalar currents

2. searches for exotic weak currents

- scalar currents
- tensor currents

3. symmetry tests

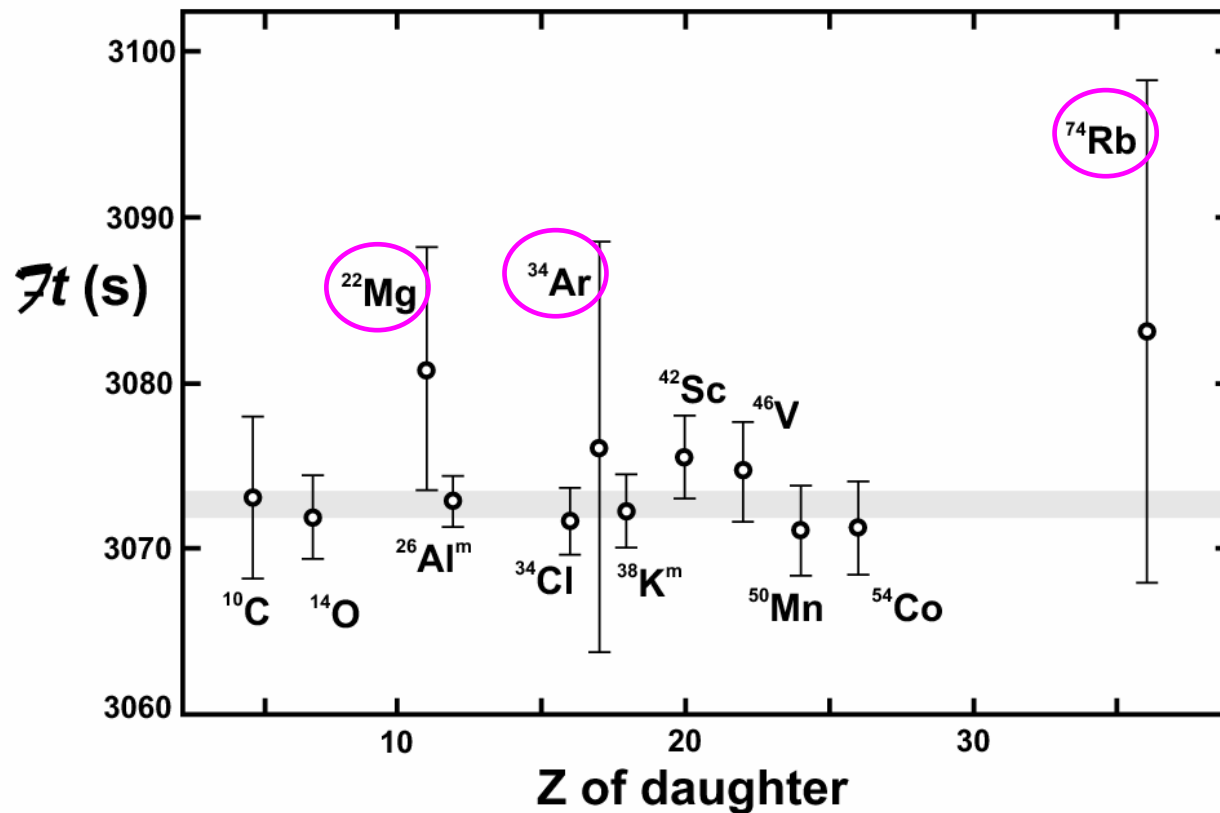
- parity
- time reversal

N. Severijns et al., Rev. Mod. Phys. 78 (2006) 991

4. searches for heavy neutrinos

1. $\mathcal{F}t$ -values of $0^+ \rightarrow 0^+$ superallowed Fermi transitions

$$\mathcal{F}t \equiv \underbrace{ft}_{\downarrow \text{Q}_{EC}, t_{1/2} \text{ and BR}} (1 + \underbrace{\delta'_R}_{\text{theory}}) (1 + \underbrace{\delta_{NS} - \delta_C}_{\text{theory}}) = \frac{K}{2G_V^2(1 + \underbrace{\Delta_R^V}_{\text{theory}})} = 3074.4(12) \text{ s} \quad (1,2)$$



1. test of CVC hypothesis

→ OK @ 4×10^{-4} level

2. test of unitarity of CKM-matrix

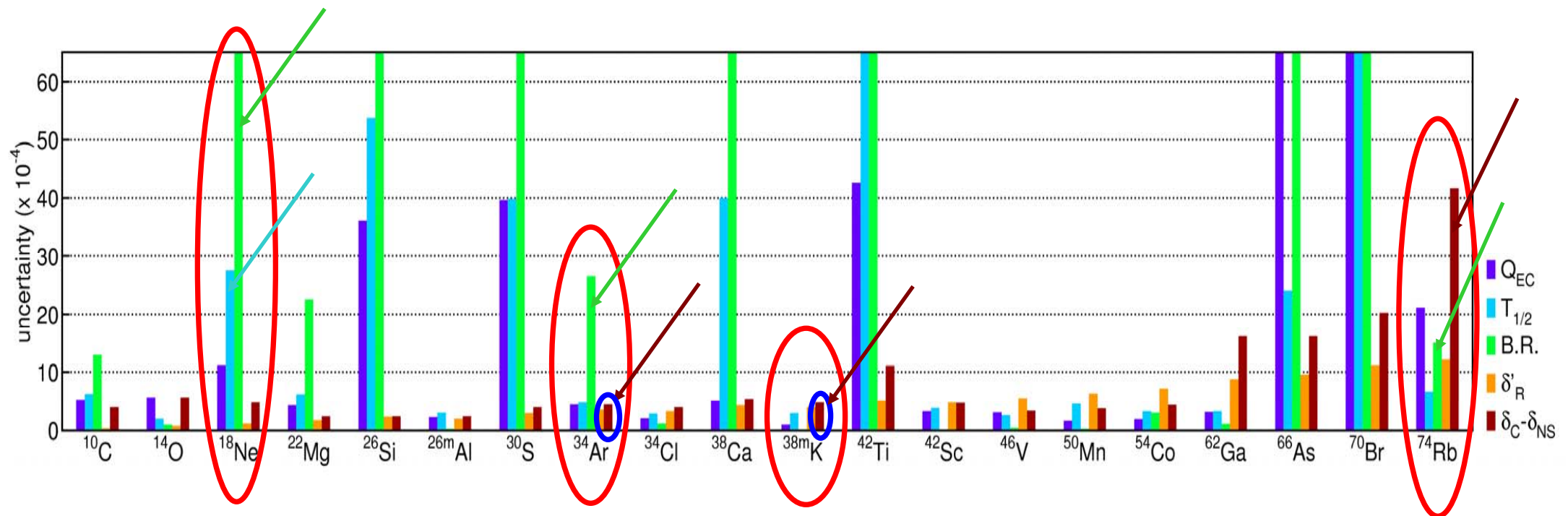
$$\sum_i V_{ui}^2 = V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 0.9987(11)$$

(with new values for V_{us})

(1) Towner and Hardy, PRL 94 (2003) 092501, PR C71 (2005) 055501
 (2) Savard et al., PRL 95 (2005) 102501

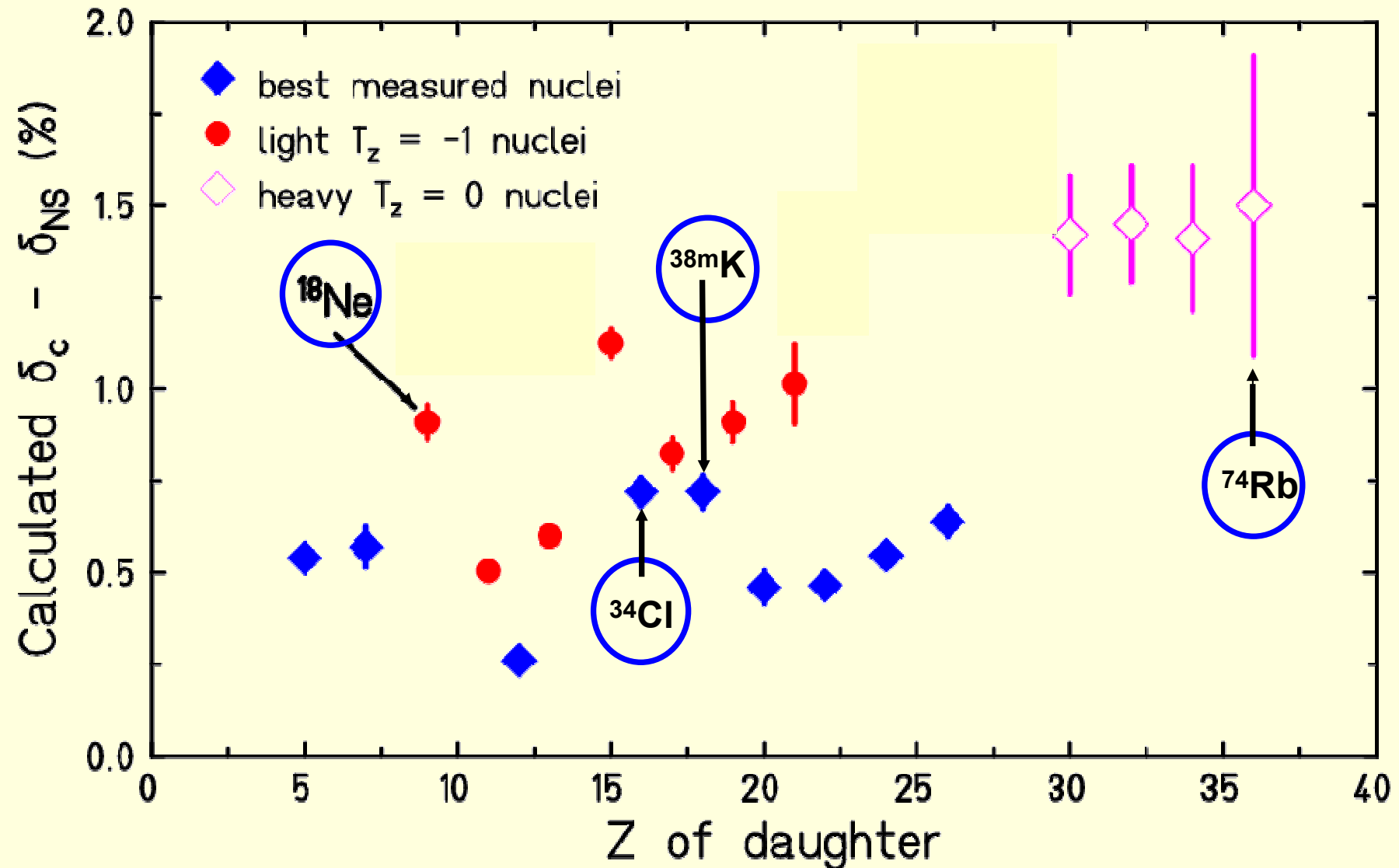
**Error budget,
required precision,
and opportunities
for MYRRHA (arrows)**

- overall precision: $Ft = (3074.4 \pm 1.2) \text{ s}$
 $\Rightarrow 4 * 10^{-4}$
 \Rightarrow single measurements of $T_{1/2}$ and BR : $< 10^{-3}$
- theoretical corrections: $\delta_C, \delta'_R \sim 1\% \rightarrow < 10\%$



- Options:**
- improve quantities indicated by green & blue arrows
 - if CVC accepted \rightarrow Ft-measurements test $\delta_C - \delta_{NS}$ from theoretical models
 - go for factor ~ 10 higher precision in Ft than available now for the 4 isotopes indicated

isospin-mixing corrections + NS radiative corrections



physics information from the $0^+ \rightarrow 0^+$ Fermi transitions

1. Conserved Vector Current hypothesis

cf. supra

2. unitarity of CKM quark-mixing matrix

cf. supra

3. right-handed (V+A) currents

$$-0.0005 < \zeta < 0.0015 \quad (90\% \text{ C.L.})$$

Left Right Symmetric models

$$W_1 = W_L \cos\zeta - W_R \sin\zeta$$

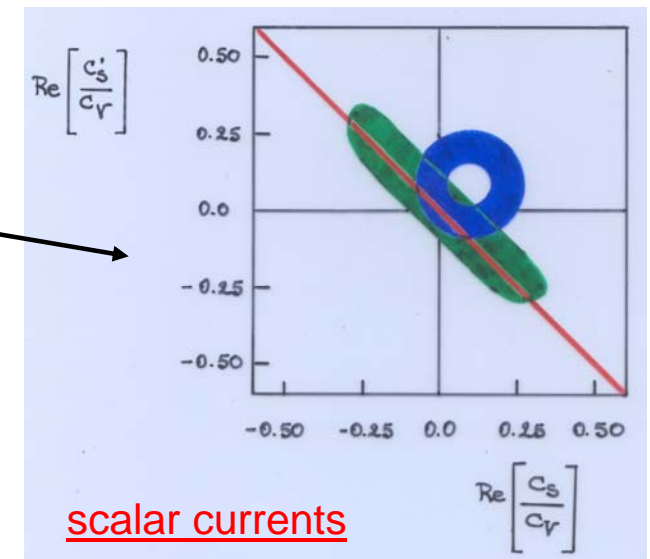
$$W_2 = W_L \sin\zeta + W_R \cos\zeta$$

$$\delta = m_1^2 / m_2^2$$

4. scalar currents

$$-0.005 < \operatorname{Re}\left(\frac{C_S + C'_S}{C_V}\right) < 0.011$$

(90% CL)

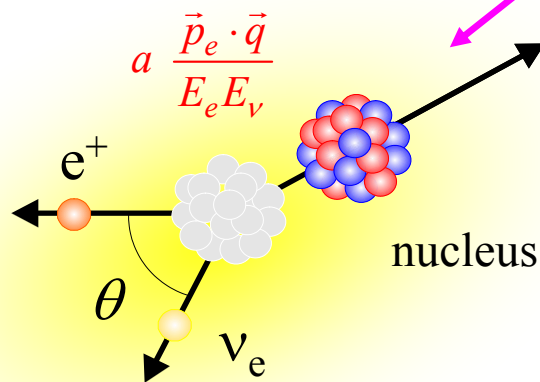


2. Searches for exotic weak currents via correlation measurements

decay rate for beta decay
of (un)polarized nuclei :

$$\omega(E, \Omega, \dots) \propto \xi \left\{ 1 + a \frac{\vec{p}_e \cdot \vec{q}}{E_e E_\nu} + b \frac{\gamma m_e}{E_e} + A \frac{\vec{J} \cdot \vec{p}_e}{J E_e} + R \frac{\vec{\sigma} \cdot \vec{J}}{J} \times \frac{\vec{p}_e}{E_e} + \dots \right\}$$

β -v correlation
Fierz interference term
($b \equiv 0$ in standard model)
 β -asymmetry
R-correlation



$\tilde{X} = \frac{X}{1 + b \frac{\gamma m_e}{E_e}} \quad (X = a, A, \dots)$
 $\gamma = \sqrt{1 - (\alpha Z)^2}$

Note: a, b, A, R, \dots depend on the coupling strengths
for the different possible weak interaction types (i.e A, V, S, T)

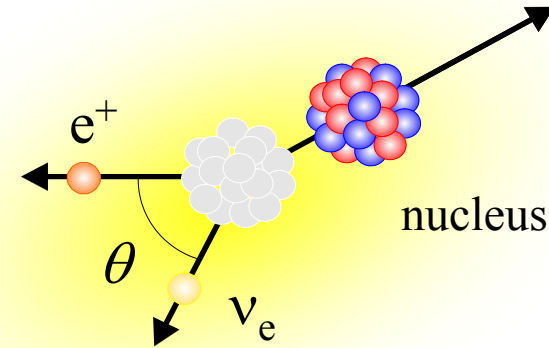
2a. $\beta\nu$ -correlation, a

measure

$$a \frac{\vec{p}_e \cdot \vec{q}}{E_e E_\nu}$$

or $\tilde{a} = \frac{a}{1 + b \frac{\gamma m_e}{E_e}}$

(with $\gamma = \sqrt{1 - (\alpha Z)^2}$)



$$a_F \cong 1 - \frac{|C_S|^2 + |C'_S|^2}{|C_V|^2}$$

$$a_{GT} \cong -\frac{1}{3} \left[1 - \frac{|C_T|^2 + |C'_T|^2}{|C_A|^2} \right]$$

$$b_F \cong \text{Re} \frac{C_S + C'_S}{C_V}$$

$$b_{GT} \cong \text{Re} \frac{C_T + C'_T}{C_A}$$

(assuming maximal P-violation and T-invariance for V and A interactions)

recoil corr. (induced form factors) $\approx 10^{-3}$; radiative corrections $\approx 10^{-4}$

traps for correlations in nuclear beta decay

isotope	trap	meas.	lab
^{21}Na	MOT	$a_F^{(1)}$	LBNL
$^{38\text{m}}\text{K}$	MOT	$a_F^{(2)}$	TRIUMF
^6He	Paul	a_{GT}	LPC/GANIL
^{35}Ar	Penning	a_F	KUL/ISOLDE
$^{21}\text{Na}, ^{19}\text{Ne}, ^{23}\text{Mg}$	MOT	a, D	KVI
^{82}Rb	MOT	A_{GT}	LANL

⁽¹⁾ = 0.5243(91) Scielzo et al. PRL 93(2004) 102501
⁽²⁾ = 0.9978(30)(37) Gorelov et al. PRL 94 (2005) 142501

N. Scielzo, S.J. Freedman et al.,

PRL 93 (2004) 102501

A. Gorelov, J. Behr et al.,

PRL 94 (2005) 142501

R. Rodriguez, O. Naviliat et al.,

NIM A565 (2006) 876

M. Beck, N. Severijns et al.,

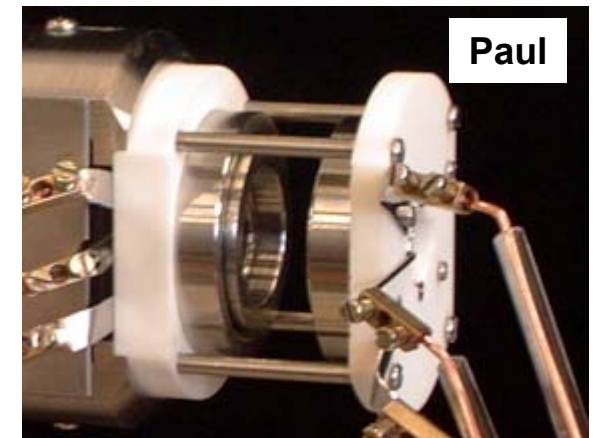
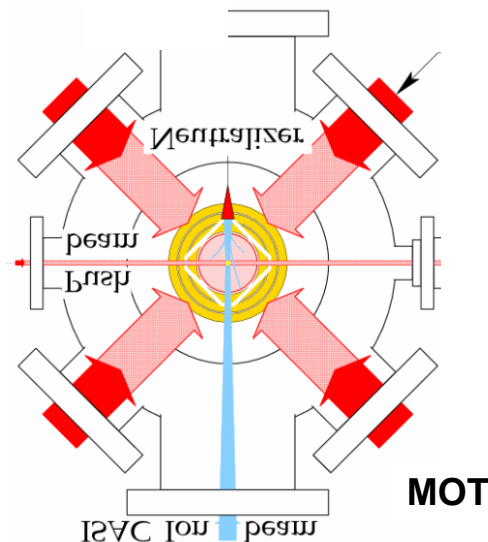
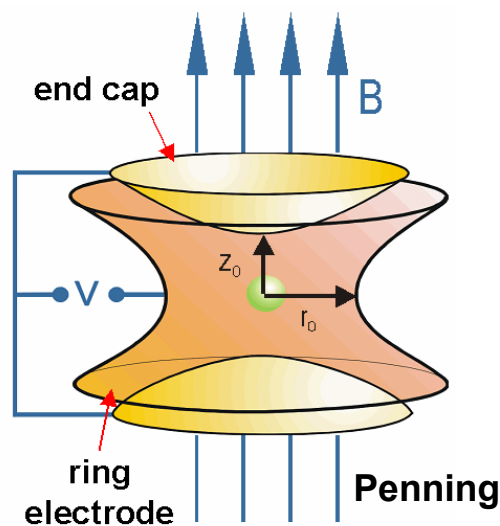
NIM A503 (2003) 567

G.P. Berg, K. Jungmann et al.,

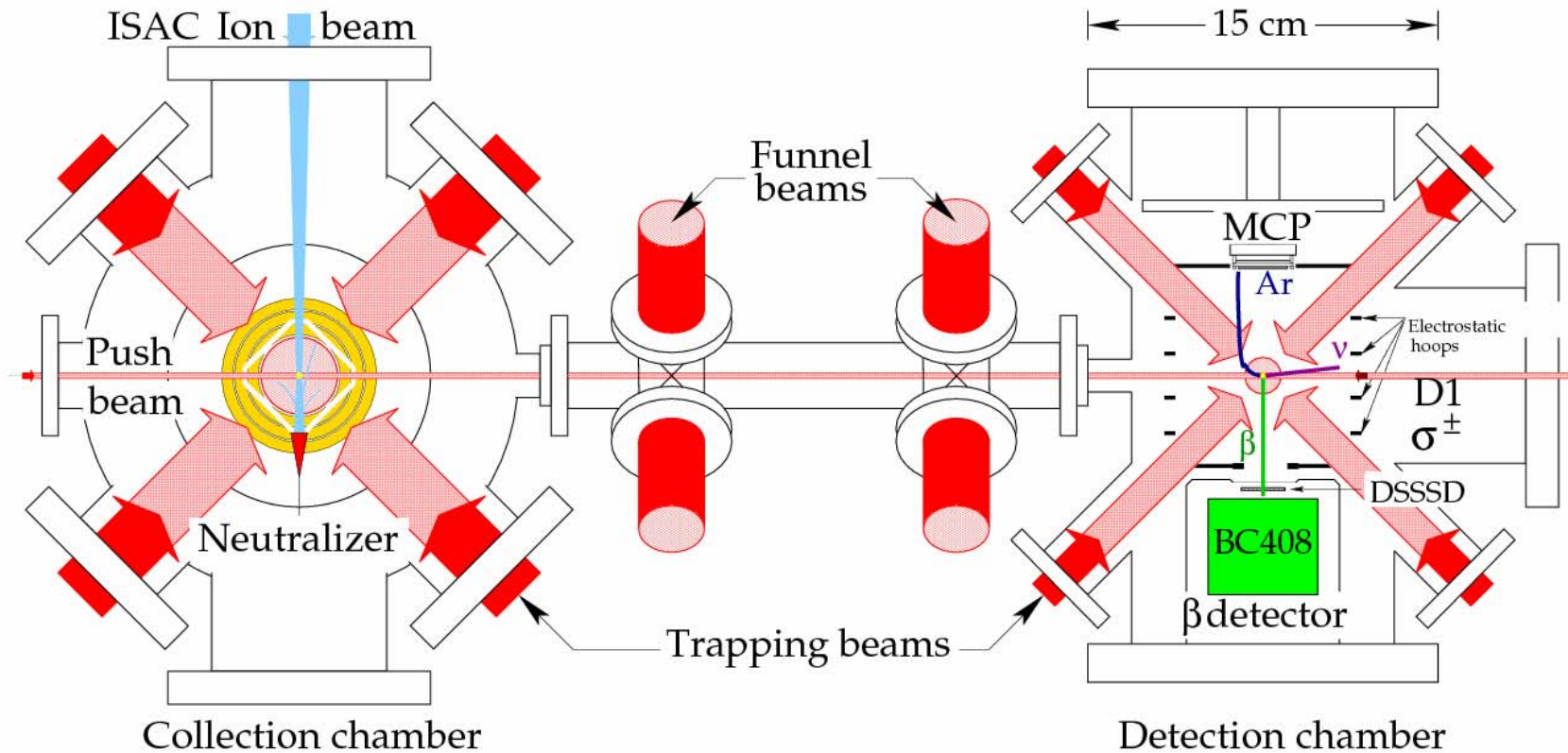
NIM B204 (2003) 52

S.G. Crane, D.J. Vieira et al.,

PRL 86 (2001) 2967



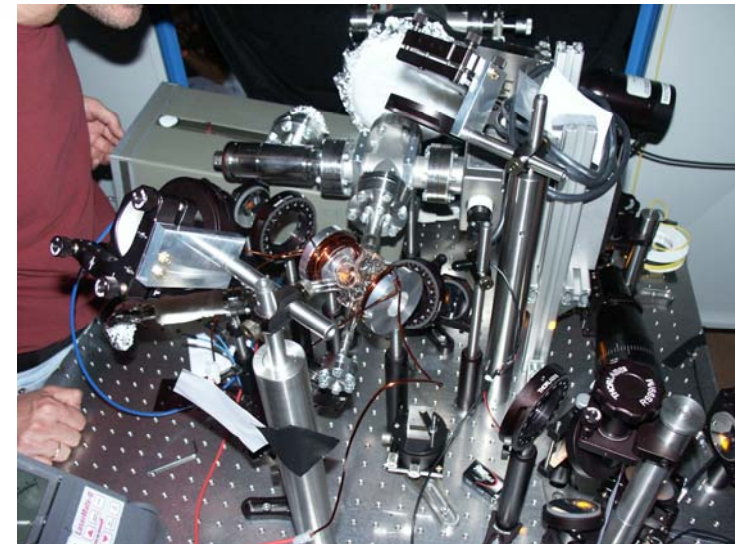
TRINAT MOT trap at TRIUMF-ISAC (Vancouver)



search for exotic scalar couplings with ^{38m}K (J. Behr et al.)

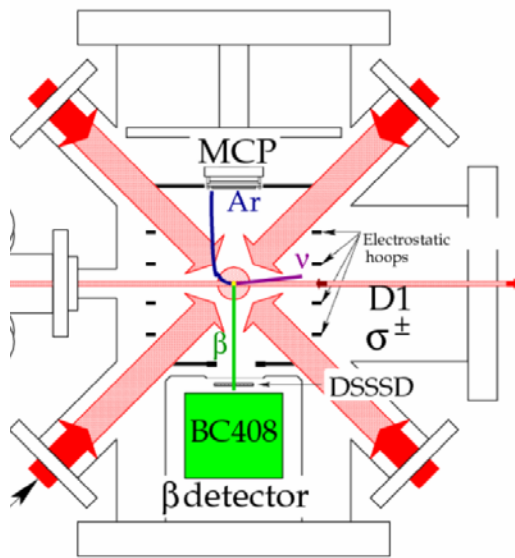


superallowed $0^+ \rightarrow 0^+$ pure Fermi transition ($t_{1/2} = 0.95$ s)

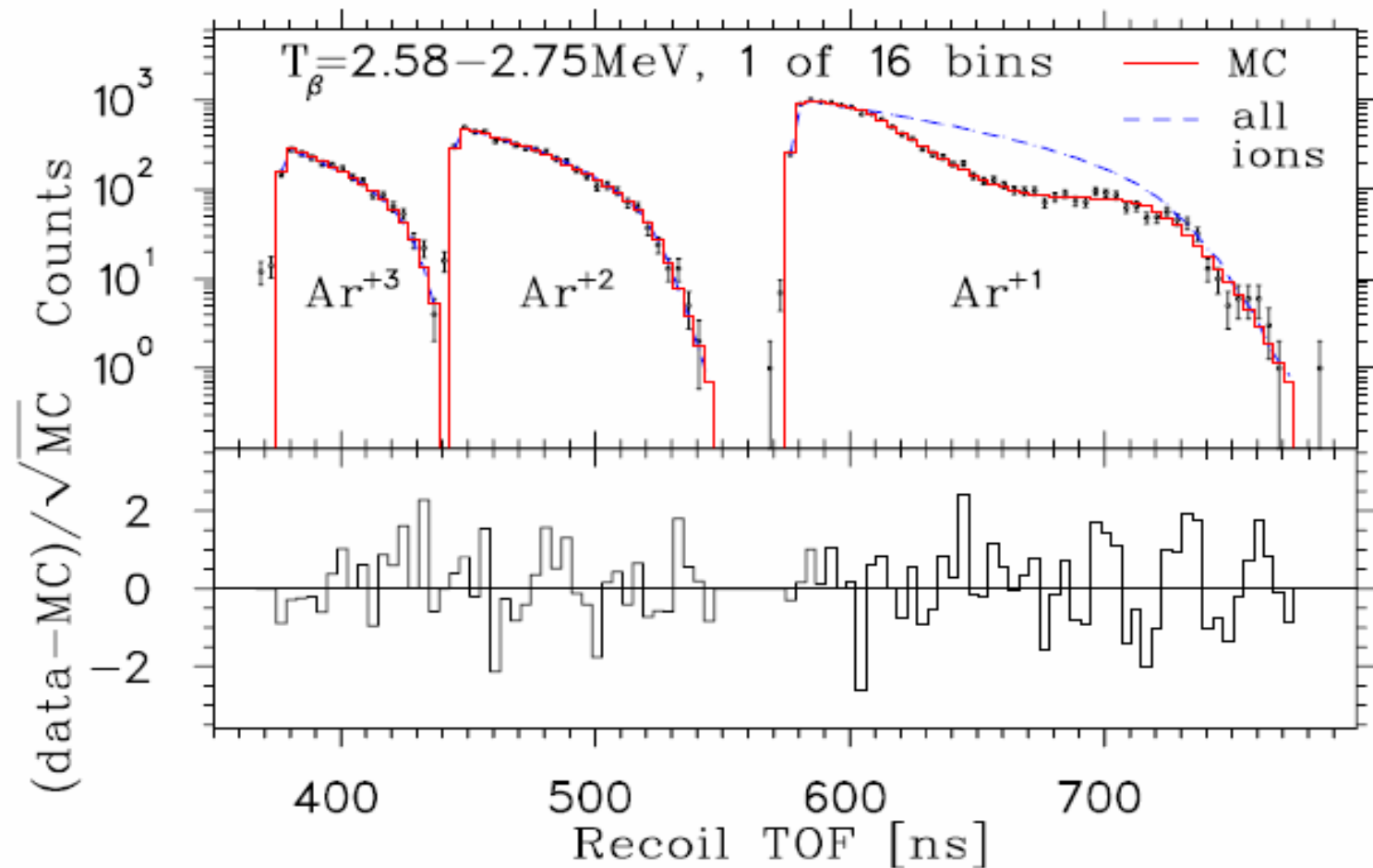


$$\tilde{a} = \frac{a}{1 + \gamma \frac{m_e}{E_e} b} = 0.9981 \pm 0.0030 \pm 0.0035 \quad (\tilde{a}_{SM} = 1) \quad \Rightarrow \quad \frac{|C_s|^2 + |C'_s|^2}{|C_V|^2} \leq 0.097$$

(90% C.L. $\cong 1.65\sigma$)

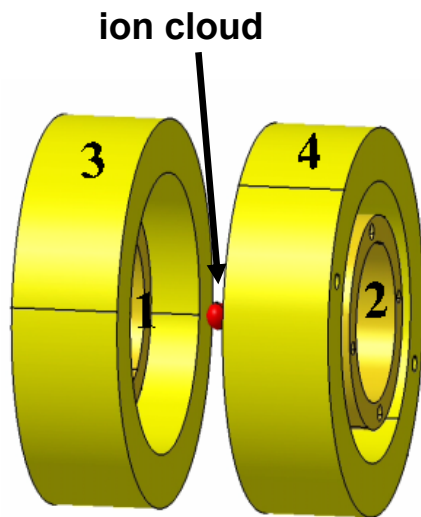
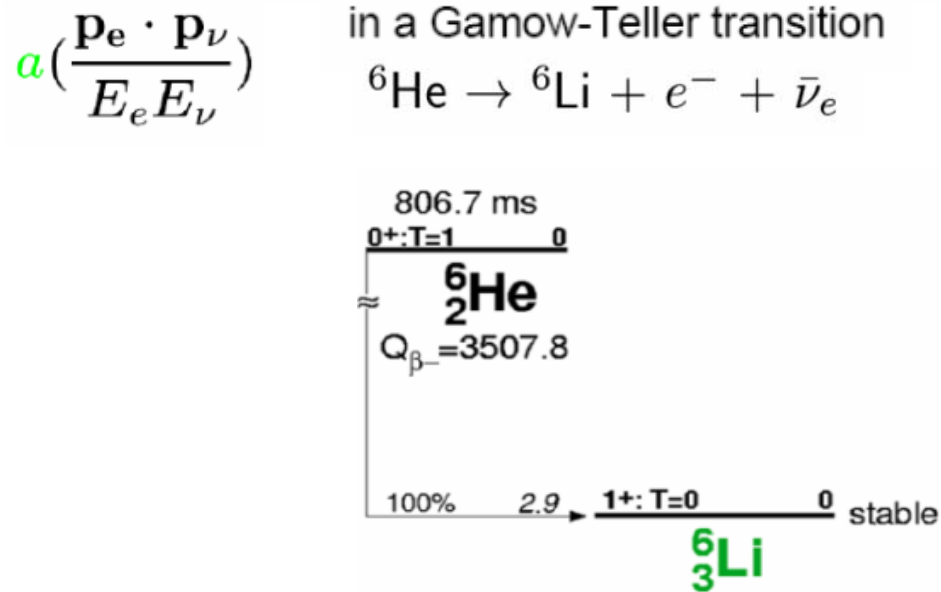


A. Gorelov, J. Behr et al.,
Phys. Rev. Lett. 94 (2005) 142501



LPC-Caen Paul trap at GANIL (O. Naviliat, G. Ban et al.)

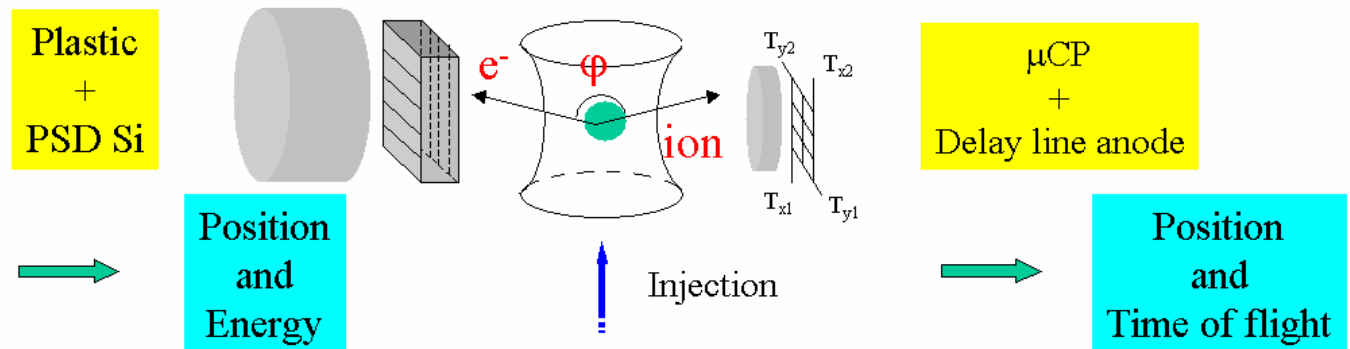
- search for exotic tensor couplings



LPC-Caen Paul trap

β - recoil coincidences

back-to-back geometry





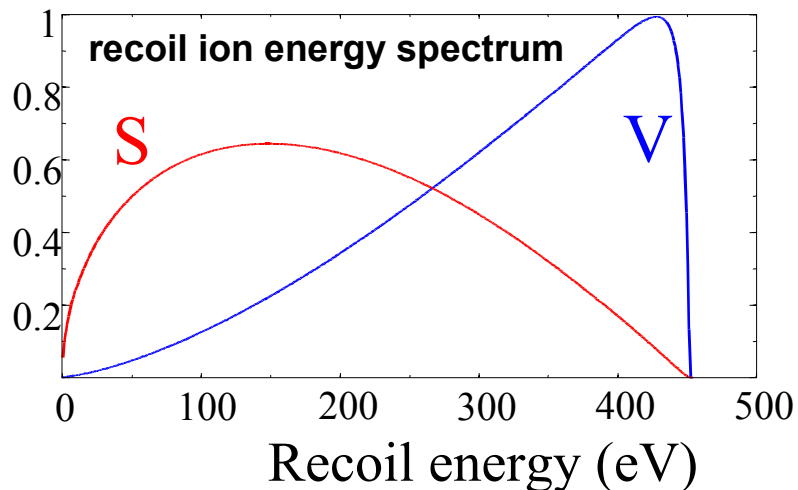
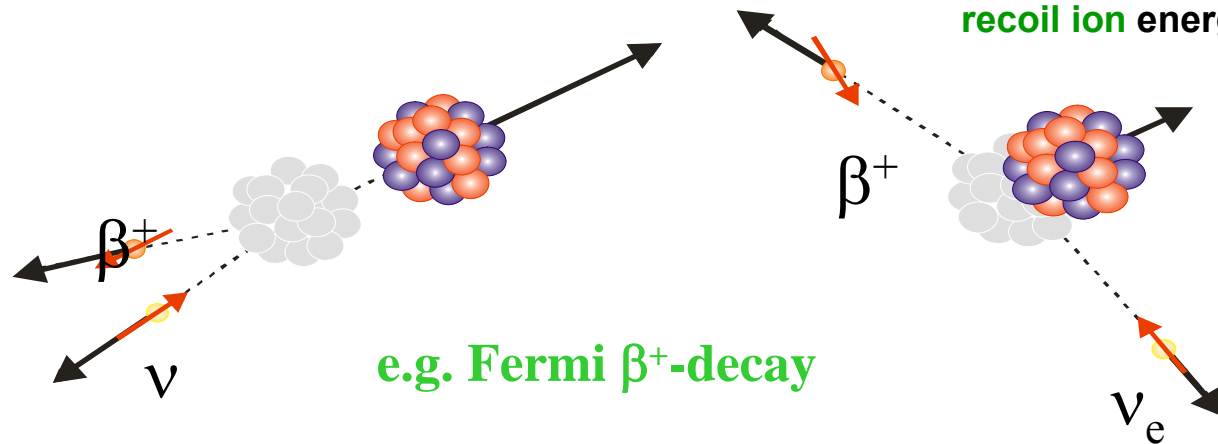
WITCH double-Penning trap system at ISOLDE-CERN

K.U.Leuven, ISOLDE-CERN, Uni Münster, GSI, NPI-Řež (Prague)

Weak Interaction Trap for CHarged particles

cooler & decay Penning traps
+ retardation spectrometer

search for exotic **scalar/tensor couplings**
in the **beta-neutrino correlation** by
recoil ion energy spectrum shape



PS-booster



ISOLDE

REXTRAP

Detector

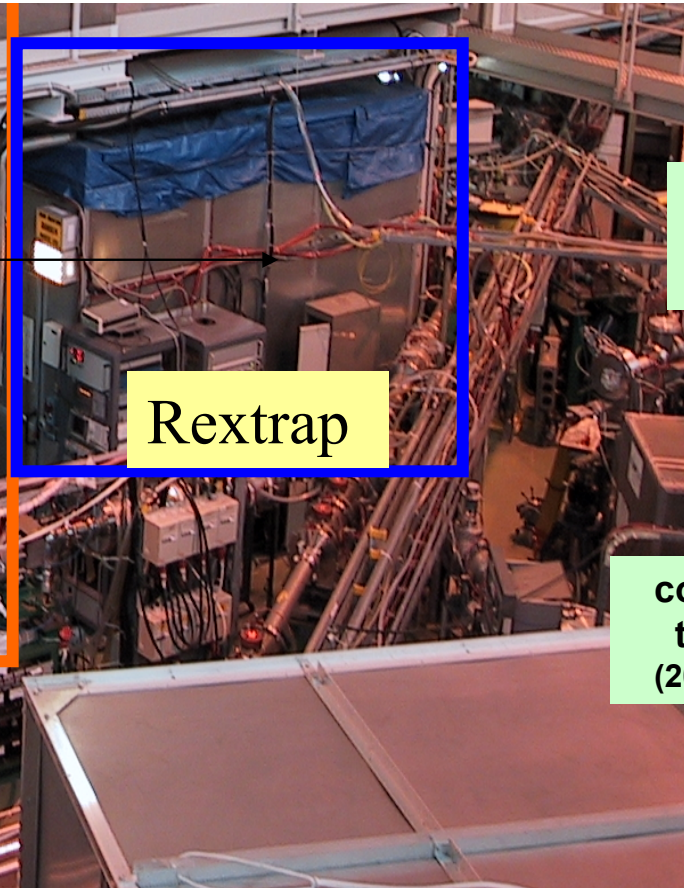
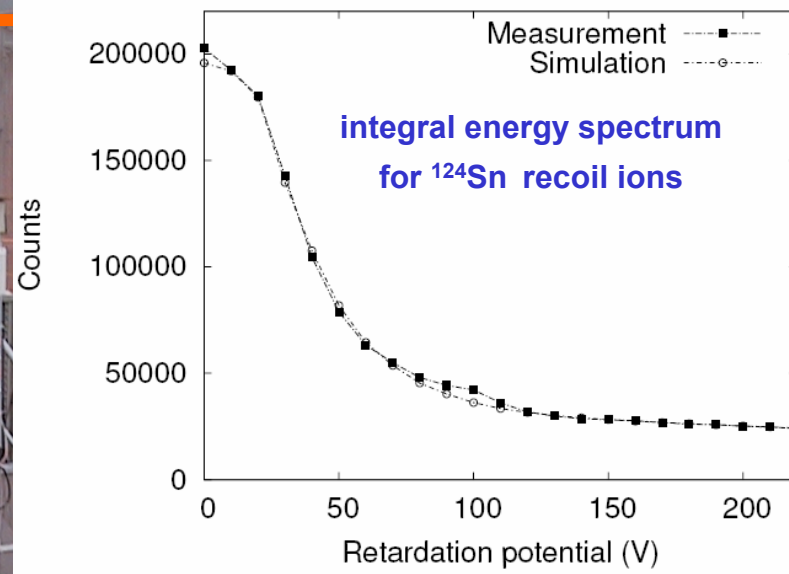
Retardation
spectrometer

decay trap

cooler trap

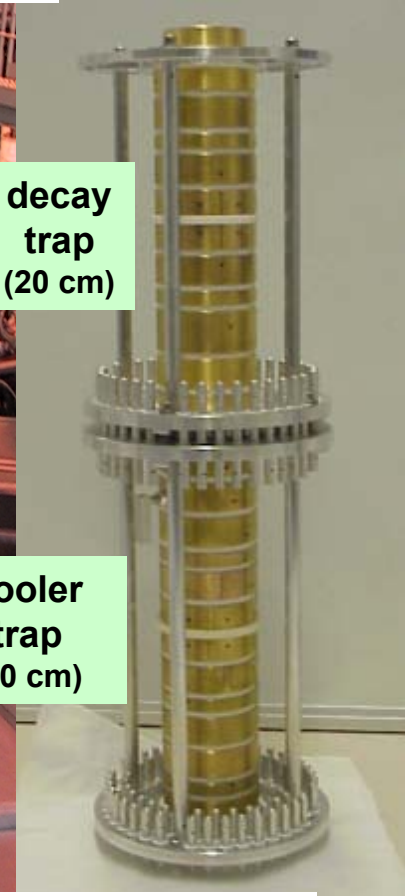
vertical
beamline

horizontal
beamline

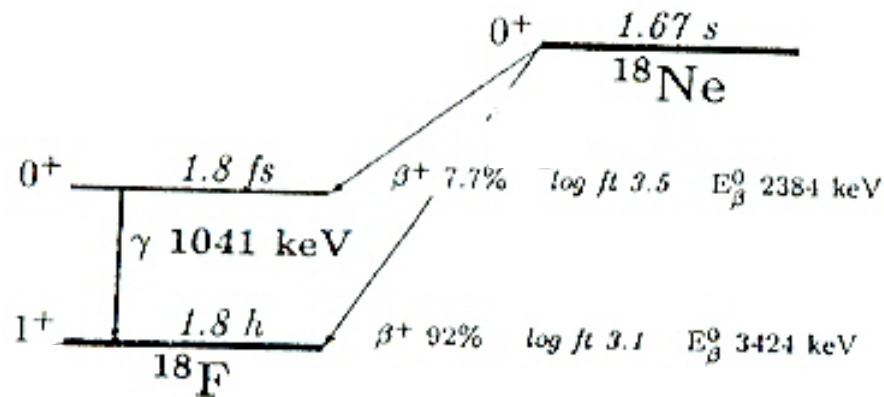


decay
trap
(20 cm)

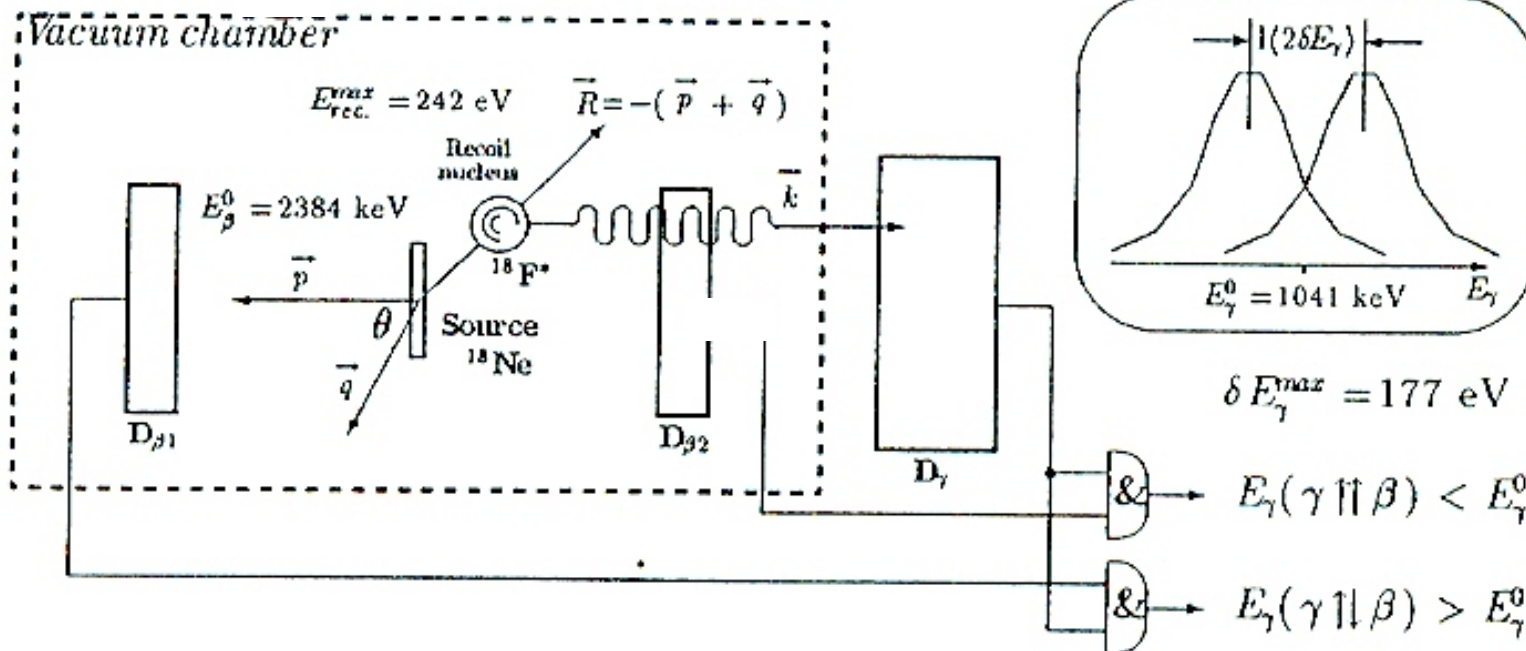
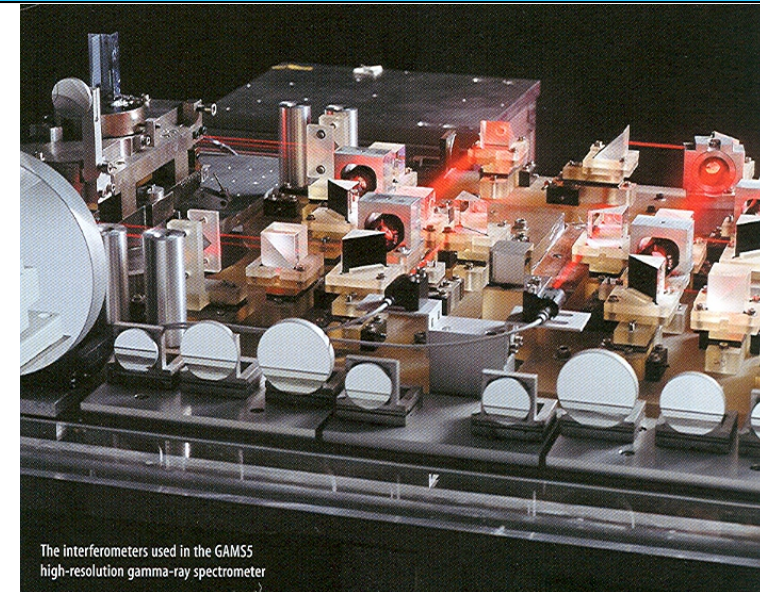
cooler
trap
(20 cm)



$\beta\nu$ -correlation from Doppler-shift of β -delayed γ -rays



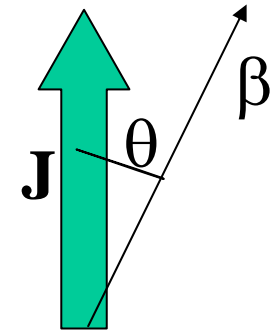
V. Egorov et al., Nucl. Phys. A 621 91997) 745



- momentum of recoil nucleus and therefore **direction of ν momentum** obtained from measured **Doppler shift** and **beta particle momentum**
- Doppler shift from **precise measurement of γ -ray energy** with a **crystal spectrometer**

2b. β asymmetry, A

$$W(\theta) = 1 + \bar{J} \cdot \frac{\bar{p}}{E_e} \tilde{A}$$



for a pure Gamow-Teller transition :

$$\tilde{A}_{GT}^{\beta^\mp} \cong \lambda_{JJ} \left[\mp 1 + \frac{\alpha Z m}{p} \text{Im} \left(\frac{C_T + C'_T}{C_A} \right) + \frac{\gamma m}{E_e} \text{Re} \left(\frac{C_T + C'_T}{C_A} \right) \right]$$

$\left[\gamma = \sqrt{1 - (\alpha Z)^2} \right]$

$-0.008 < \text{Im} (C_T + C'_T) / C_A < 0.014$ (90% CL) from ^8Li @ PSI, R. Huber et al., PRL 90 (2003) 202301

$\Delta A = 0.01 \rightarrow$ (for $\gamma m / E_e \cong 0.5$) $\text{Re} [(C_T + C'_T) / C_A] < 0.033$ (90% CL)

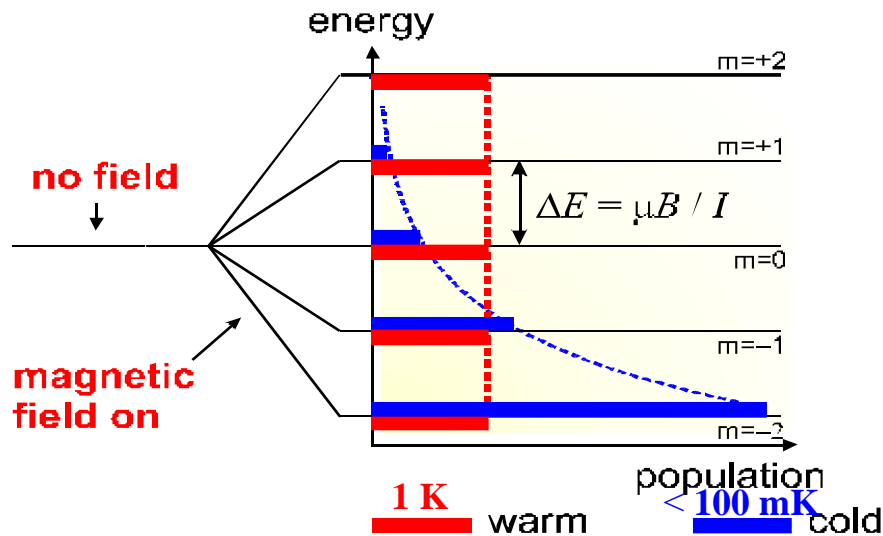
(assuming maximal P-violation and T-invariance for V and A interactions)

recoil corr. (induced form factors) $\approx 10^{-3}$; radiative corrections $\approx 10^{-4}$ / A_{GT} independent of nuclear matrix elements

Low Temperature Nuclear Orientation + Geant 4

(K.U.Leuven, NICOLE-ISOLDE, NPI Rez-Prague, Uni Bonn)

F. Wauters, I. Kraev, D. Zakoucky, N. Severijns et al.

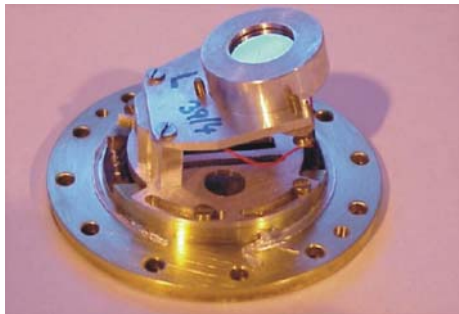
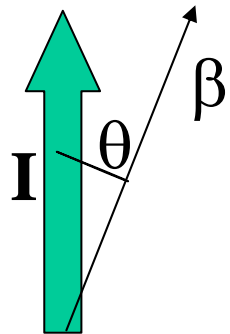


$$W(\theta) = \frac{N(\theta)_{\text{pol}}}{N(\theta)_{\text{unpol}}} = 1 + \tilde{A}_{\text{GT}}^{\beta^{\mp}} P \left(\frac{v}{c} Q \cos\theta \right)$$

(polarization P from anisotropy of γ -rays) **Geant 4**

Leuven: $^{60}\text{CoCu}$, $B_{\text{ext}} = 13 \text{ T}$

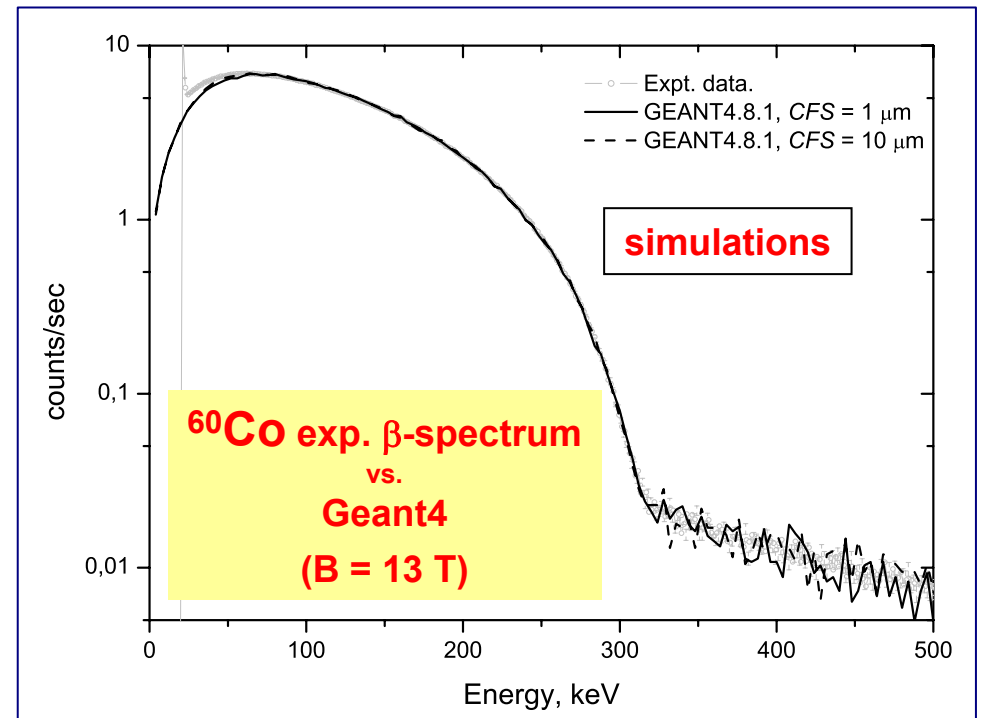
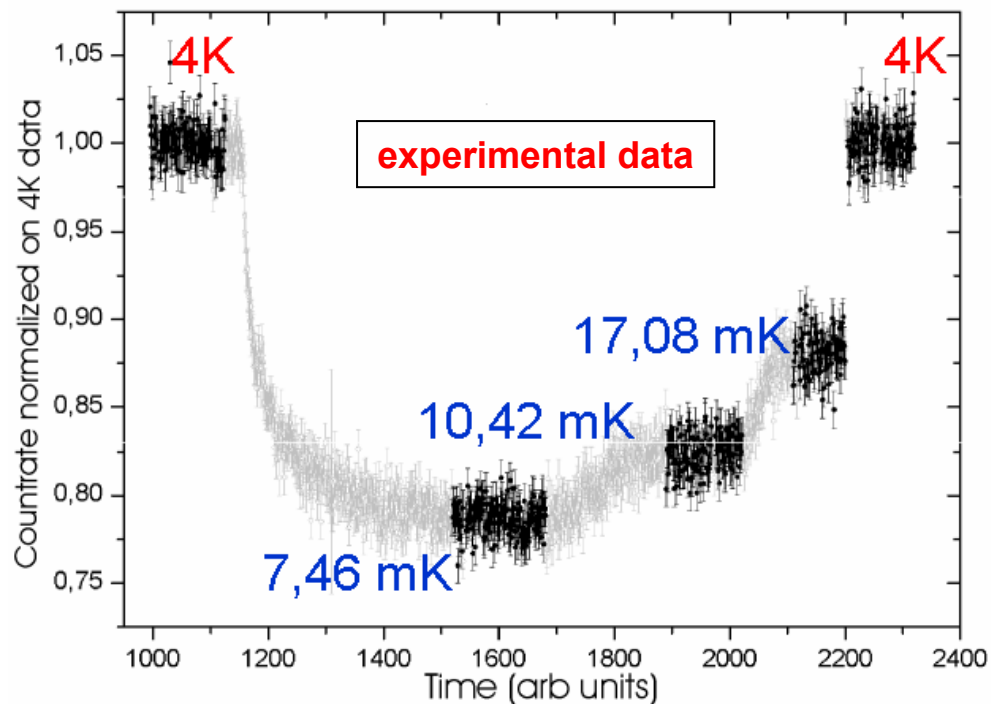
ISOLDE: $^{63}\text{CuFe}$, $B_{\text{hf}} = 22 \text{ T}$



Analysis:

$$\frac{[W(\theta) - 1]_{\text{exp}}}{[W(\theta) - 1]_{\text{sim}}} = \frac{\left[\tilde{A}_{\text{GT}}^{\beta^{\text{m}}} P \frac{v}{c} Q \cos\theta \right]_{\text{exp}}}{\left[\tilde{A}_{\text{GT,SM}}^{\beta^{\mp}} P \frac{v}{c} Q \cos\theta \right]_{\text{sim}}} = \frac{\tilde{A}_{\text{GT}}^{\beta^{\mp}}}{\tilde{A}_{\text{GT,SM}}^{\beta^{\mp}}}$$

IS431-experiment



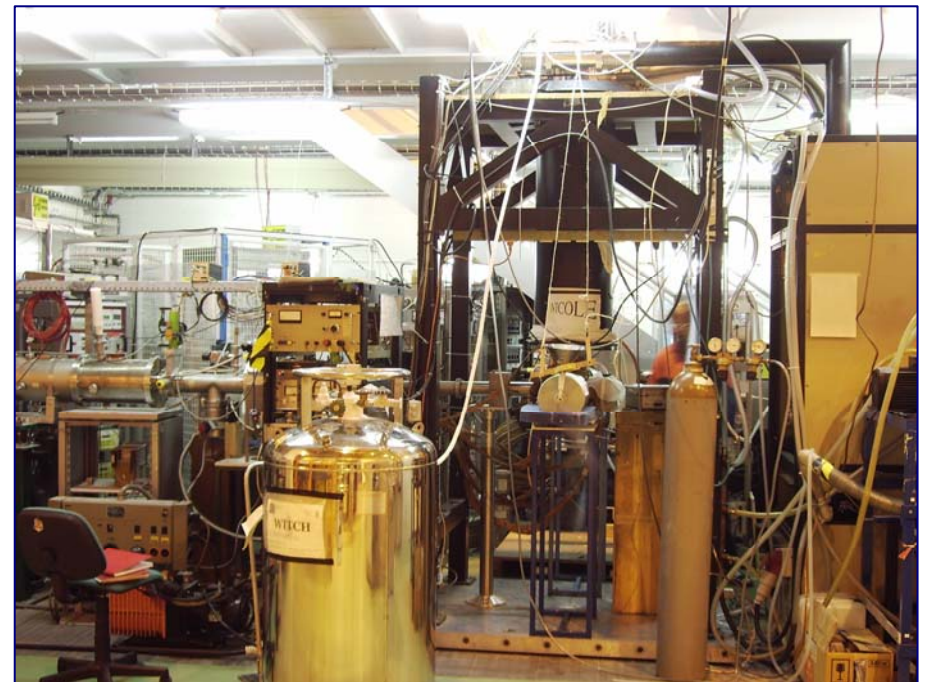
From ratio $\frac{[W(\theta)-1]_{\text{exp}}}{[W(\theta)-1]_{\text{Geant}}}$ get $\tilde{A}_{\text{exp}} / \tilde{A}_{\text{SM}}$

preliminary results :

$$\tilde{A}_{\text{exp}} / \tilde{A}_{\text{SM}} = 1.021(12) \text{ for } {}^{60}\text{Co}$$

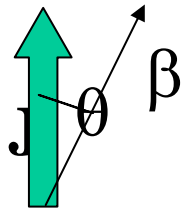
$$= 0.991(19) \text{ for } {}^{114}\text{In}$$

and data for ${}^{63}\text{Cu}$ under analysis



3. Symmetry tests - parity violation

3a. β asymmetry, A



$$W(\theta) = 1 + \bar{J} \cdot \frac{\bar{p}}{E_e} \tilde{A}$$

for a pure Gamow-Teller transition :

$$\tilde{A}_{GT}^{\beta^\mp} \cong \mp \lambda_{JJ} \left[1 - 2(\delta + \zeta)^2 \right]$$

(assuming T-invariance for V and A interactions, and no tensor component)

$$\Delta A = 0.002 \rightarrow M(W_R) < 400 \text{ GeV}/c^2 \quad (90\% \text{ CL})$$

$$\Delta A = 0.001 \rightarrow M(W_R) < 475 \text{ GeV}/c^2 \quad (90\% \text{ CL})$$

present 90% CL lower limit is $M(W_R) < 320 \text{ GeV}/c^2$ (Severijns et al., NP A 629 (1998) 423c)

“probing the $500 \text{ GeV}/c^2$ region would provide new information on several extensions of the Standard Model “
(Herczeg, Prog. Part. Nucl. Phys. 46 (2001) 413)

Manifest Left-Right
Symmetric models

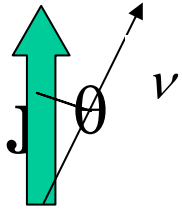
$$W_1 = W_L \cos \zeta - W_R \sin \zeta$$

$$W_2 = W_L \sin \zeta + W_R \cos \zeta$$

$$\delta = m_1^2 / m_2^2 ; \quad \zeta \cong 0.001$$

recoil corr. (induced form factors) $\approx 10^{-3}$; radiative corrections $\approx 10^{-4}$ / A_{GT} independent of nuclear matrix elements

3b. ν asymmetry, B



$$W(\theta) = 1 + \bar{J} \cdot \frac{\bar{q}}{E_e} \tilde{B}$$

$$\tilde{B}_{GT}^{\beta^\mp} \cong \pm \lambda_{JJ} \left[1 - 2(\delta + \varsigma)^2 \right] = -\tilde{A}_{GT}^{\beta^\mp}$$

$$\frac{B^{\text{exp}}}{B^{\text{SM}}}({}^{37}\text{K}) = 0.981 \pm 0.020(\text{stat}) \pm 0.013(\text{syst}) \quad \left(\text{in about 4 days of beam time ;} \right.$$

D. Melconian et al., Phys. Lett. B 649 (2007) 370)

can be reduced by factor of about 3 to 4 !

then to be reduced by factor of about 6 to 7
to be about equal to systematic error !

3. Symmetry tests - time reversal violation

- **D correlation** :
$$D \frac{\vec{J} \cdot (\vec{p}_e \times \vec{p}_\nu)}{E_e E_\nu}$$

- sensitive to time reversal violating **V, A interactions**
- only measured for **neutron** and for **¹⁹Ne** till now (always statistics limited !)

$D = -0.0004(6)$
(several authors, 1958 - 2004)

$D = 0.0001(6)$
(F. Calaprice et al., 1969 - 1984)

- **R correlation** :
$$R \frac{\vec{J} \cdot (\vec{\sigma} \times \vec{p}_e)}{E_e E_\nu}$$

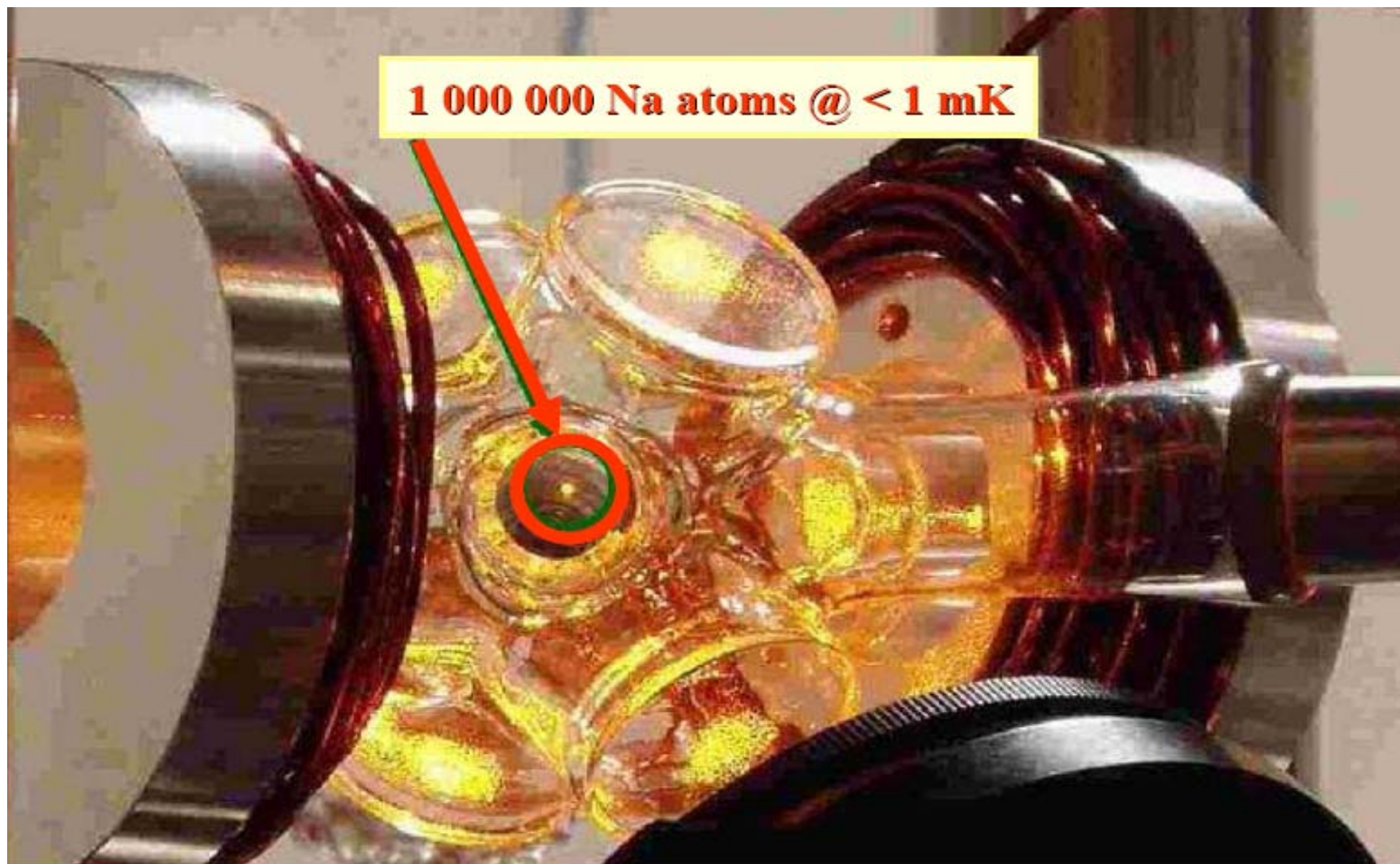
- sensitive to time reversal violating **S, T interactions**
- only measured for **neutron**, **⁸Li** and **¹⁹Ne** till now

$R = 0.007(19)$
(preliminary)
K. Bodek et al.,
to be published

$R = 0.0009(22)$
R. Huber et al.,
PRL 90 (2003) 202301

$R = 0.079(53)$
F. Schneider et al.,
PRL 51 (1983) 1239

In preparation: D(^{21}Na) in MOT optical trap at KVI-Groningen



4. Searches for heavy neutrinos

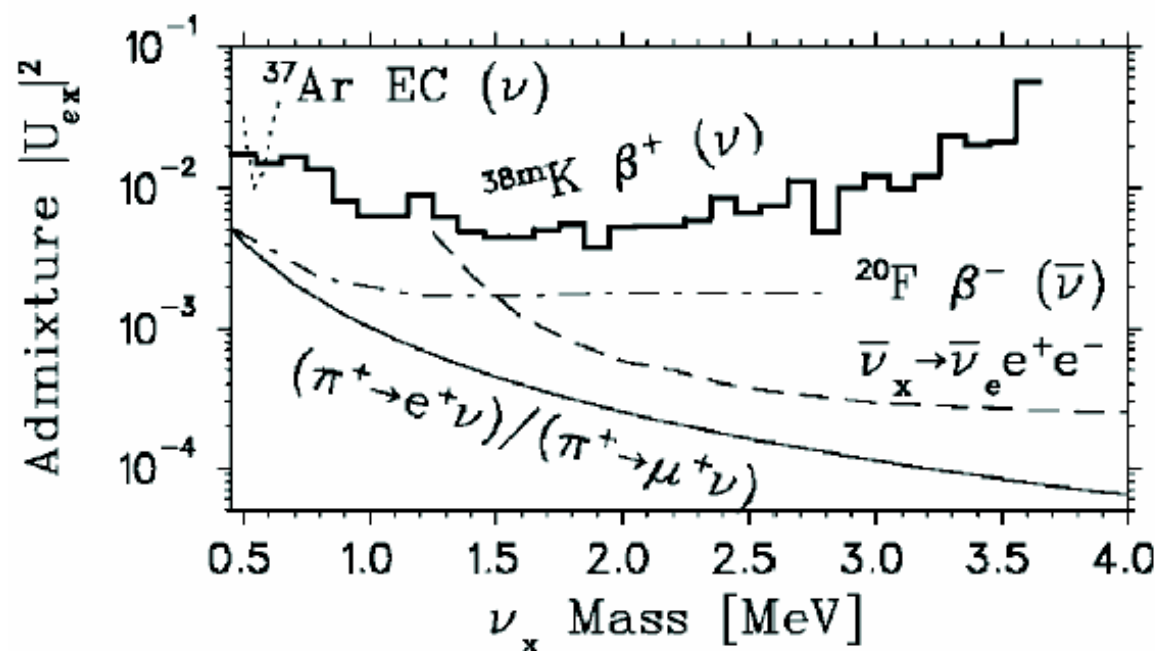
- recoil energy for nucleus that has emitted heavy neutrino is lower than for light one
 → recoil ion energy in beta decay probes existence of heavy neutrinos
 that would mix (with amplitude U_{ex}) with light neutrino :

$$|\nu_e\rangle = \sqrt{1 - |U_{ex}|^2} |\nu_0\rangle + U_{ex} |\nu_x\rangle$$

- **current best result in nuclear beta decay**

from 38mK →

(Trinczek et al., PRL 90 (2003) 012501)



- e.g. heavy neutrino search with the WITCH spectrometer :

decay : ^{144}Eu (10.2 s) \rightarrow ^{144}Sm

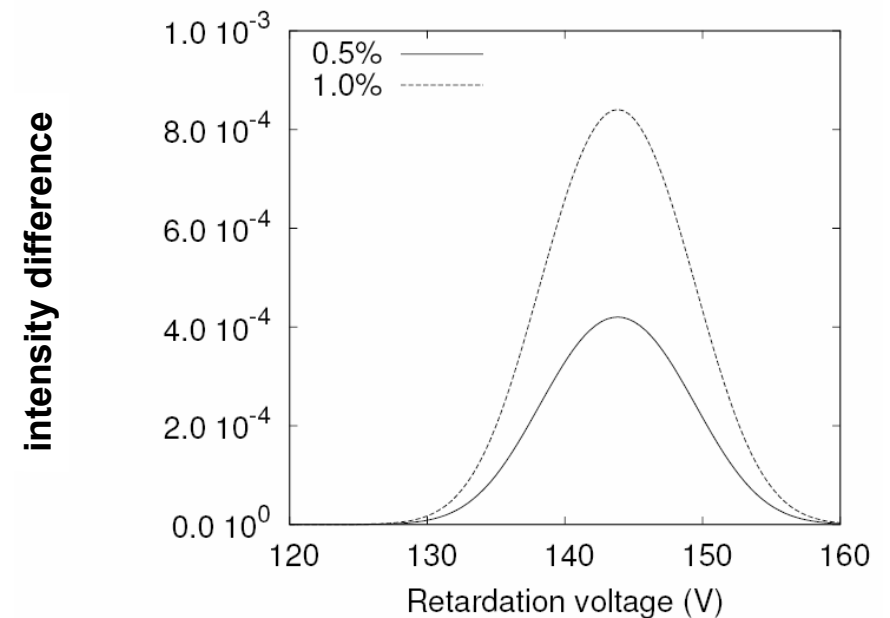
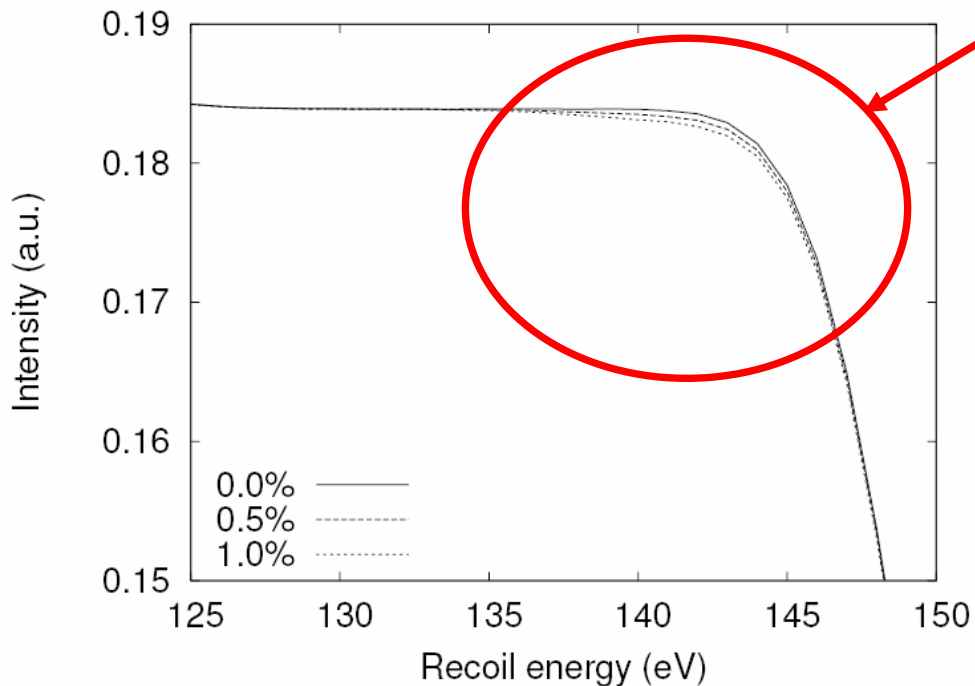
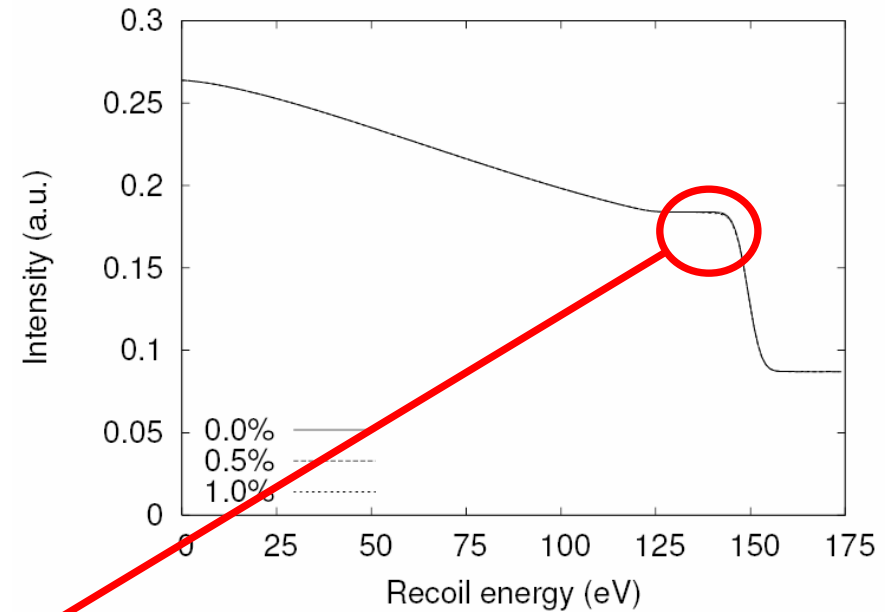
EC-branching : 9.7%

Q_{EC} -value : 6.3 MeV

beta recoil endpoint : 125 eV

EC($m_\nu = 0$) recoil peak : 149 eV

& search for peak at e.g. 138 eV
with 0.5% or 1% admixture



1. *ft*-values

→ $0^+ \rightarrow 0^+$ transitions (test CVC, unitarity test, right-handed currents, scalar currents, test nuclear structure corrections, ...)

$T_{1/2}$ and BR for ^{18}Ne , ^{34}Ar , $^{38\text{m}}\text{K}$ and ^{74}Rb

2. searches for exotic weak currents (scalar and/or tensor currents)

-
- atom traps (e.g. ^{21}Na , ^{37}K , $^{38\text{m}}\text{K}$), Penning traps (e.g. ^{35}Ar), Paul traps (e.g. ^6He),
 - beta asymmetry measurements (e.g. ^{19}Ne),
 - but also Doppler-shift of gamma-rays (e.g. ^{18}Ne , ^{35}Ar) with a crystal spectrometer

3. symmetry tests

- parity
 - beta asymmetry measurements (e.g. ^{18}Ne)
 - neutrino asymmetry in nuclear beta decay (e.g. ^{21}Na , ^{37}K)
- time reversal
 - *D* correlation ($\mathbf{J} \cdot \mathbf{p}_e \mathbf{x} \mathbf{p}_\nu$; V,A) - (e.g. ^{19}Ne)
 - *R* correlation ($\boldsymbol{\sigma} \cdot \mathbf{J} \mathbf{x} \mathbf{p}_e$; S,T) - (e.g. ^8Li , ^{19}Ne)

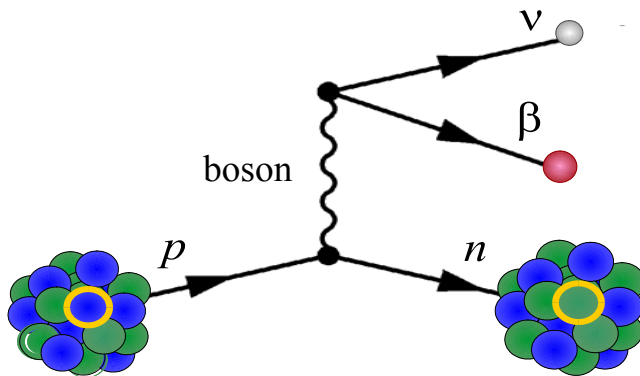
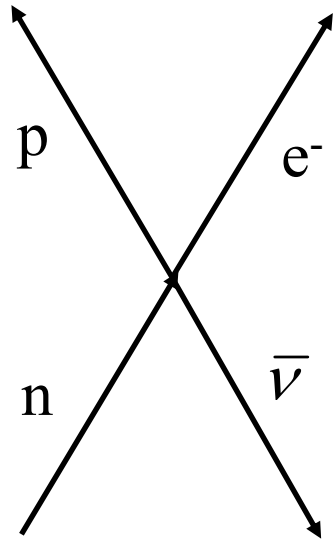
4. searches for heavy neutrinos

Motivation:

- long measuring times
- high precision
- good knowledge of apparatus required (systematic effects)

STRUCTURE OF THE WEAK INTERACTION IN NUCLEAR BETA DECAY

β -decay Hamiltonian (Lee & Yang) :



$$\begin{aligned}
 H_{\beta}/g \propto & (\bar{p} \mathbf{1} n) [\bar{e} \mathbf{1} (C_S + C'_S \gamma_5) \nu] \\
 & + (\bar{p} \gamma_{\mu} n) [\bar{e} \gamma_{\mu} (C_V + C'_V \gamma_5) \nu] \\
 & + \frac{1}{2} (\bar{p} \sigma_{\mu\nu} n) [\bar{e} \sigma_{\mu\nu} (C_T + C'_T \gamma_5) \nu] \\
 & - (\bar{p} \gamma_{\mu} \gamma_5 n) [\bar{e} \gamma_{\mu} \gamma_5 (C_A + C'_A \gamma_5) \nu] \\
 & + \cancel{(\bar{p} \gamma_5 n) [\bar{e} \gamma_5 (C_P + C'_P \gamma_5) \nu]} \\
 & \quad \quad \quad \approx 0
 \end{aligned}$$

with γ_i ($i = 1, 2, 3, 4$) Dirac matrices ($\gamma_5 = \gamma_1 \gamma_2 \gamma_3 \gamma_4$)

and $\sigma_{\mu\nu} = -\frac{i}{2}(\gamma_{\mu} \gamma_{\nu} - \gamma_{\nu} \gamma_{\mu})$

P-violation if $C_i \neq 0$ and $C'_i \neq 0$

T-violation if $\text{Im}(C_i^{(0)} / C_j) \neq 0$

the Standard Model and beyond:

- * $C_V = 1$ (CVC)
- * $C_A = -1.27$ ($g_A/g_V = -1.2699(7)$ from n-decay)
- * $C_V' = C_V$ & $C_A' = C_A$ (maximal P-violation)

- * $C_S = C_S' = C_T = C_T' = C_P = C_P' \equiv 0$ (only V- and A-currents)

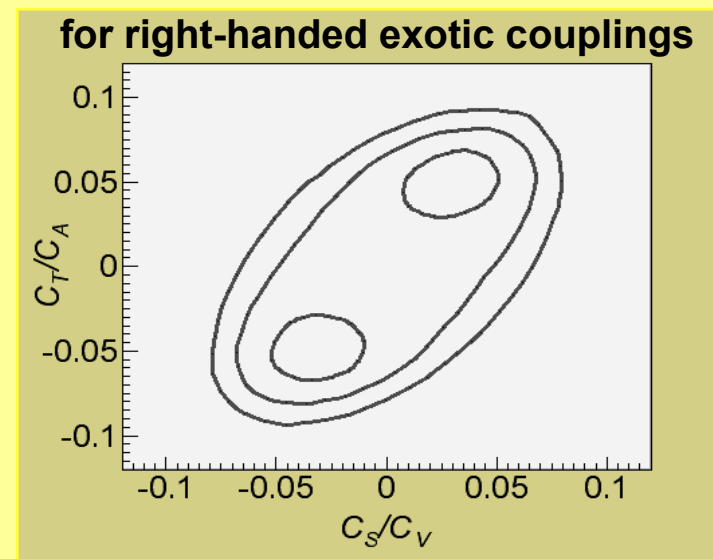
experimental upper limits:

(neutron and nuclear β -decay)

$$\left| C_T^{(')} / C_A \right| < 0.09$$

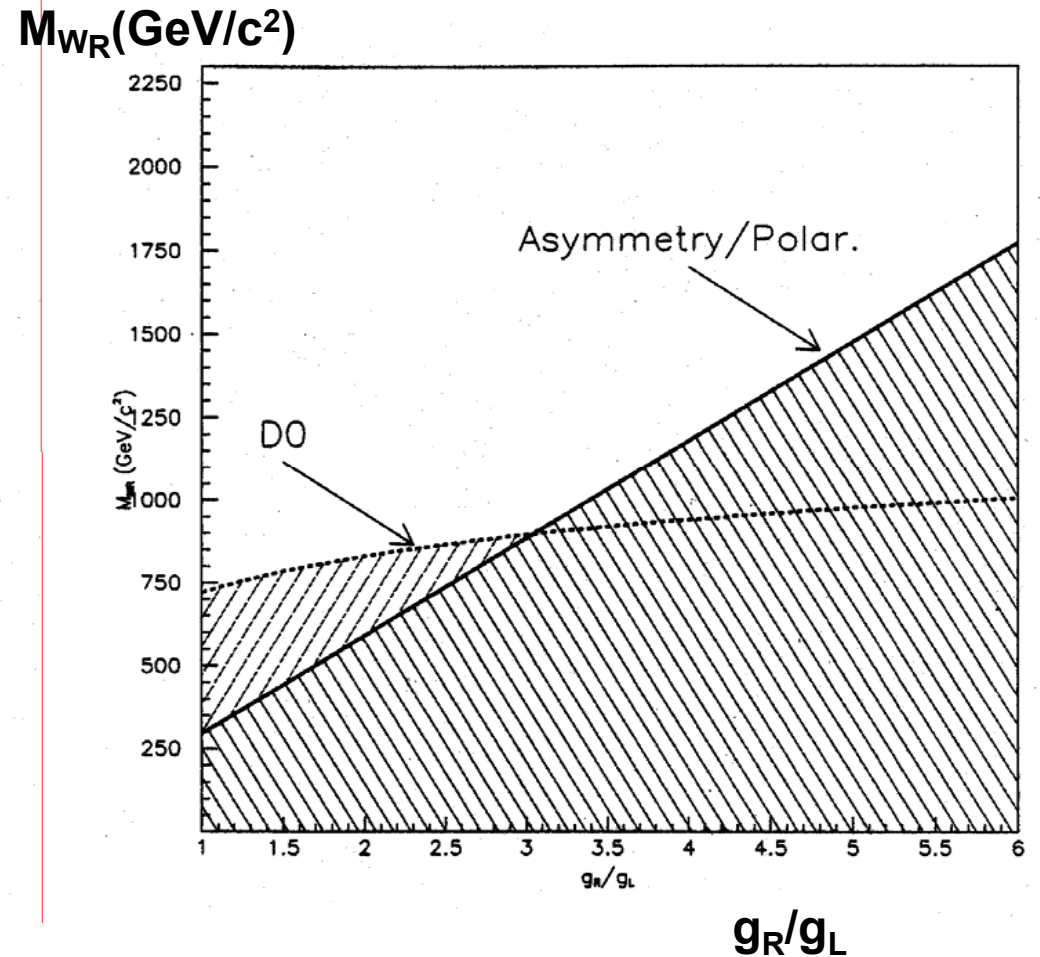
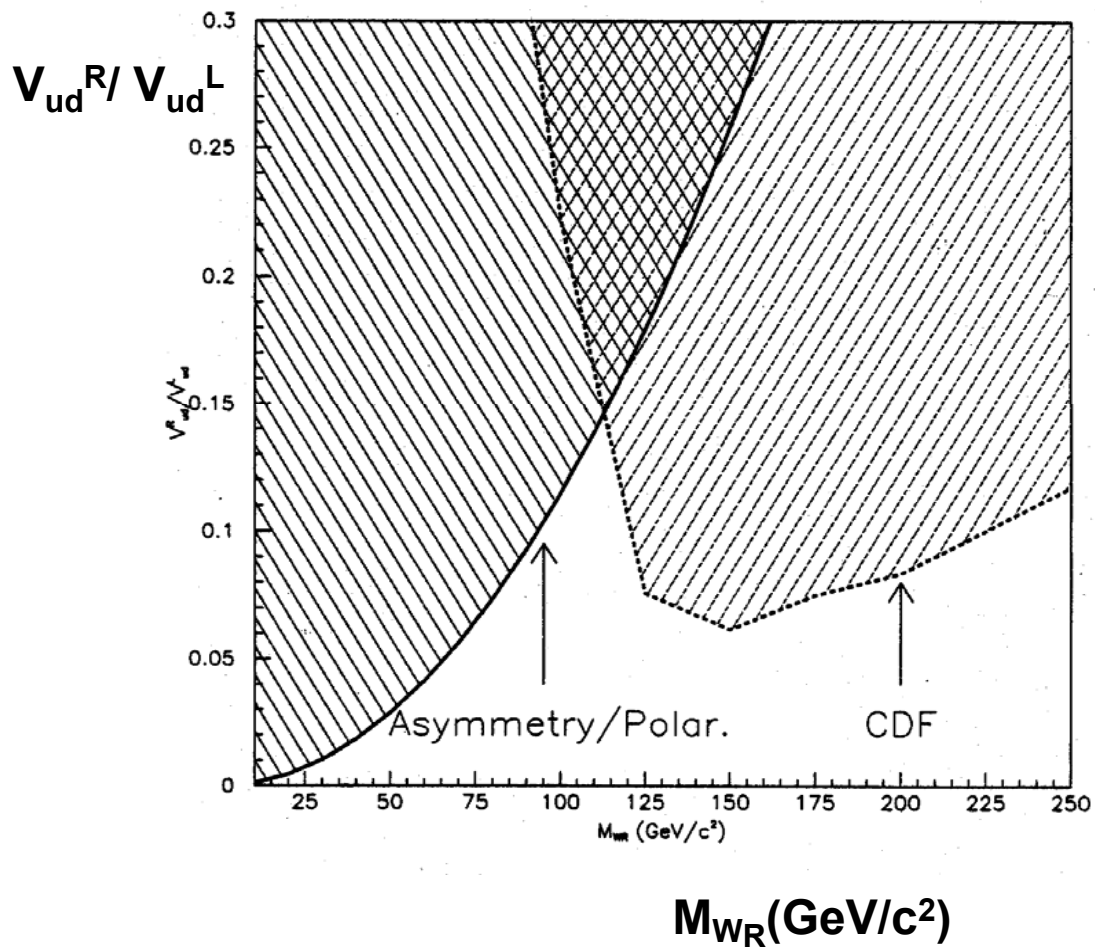
$$\left| C_S^{(')} / C_V \right| < 0.07 \quad (95\% \text{CL})$$

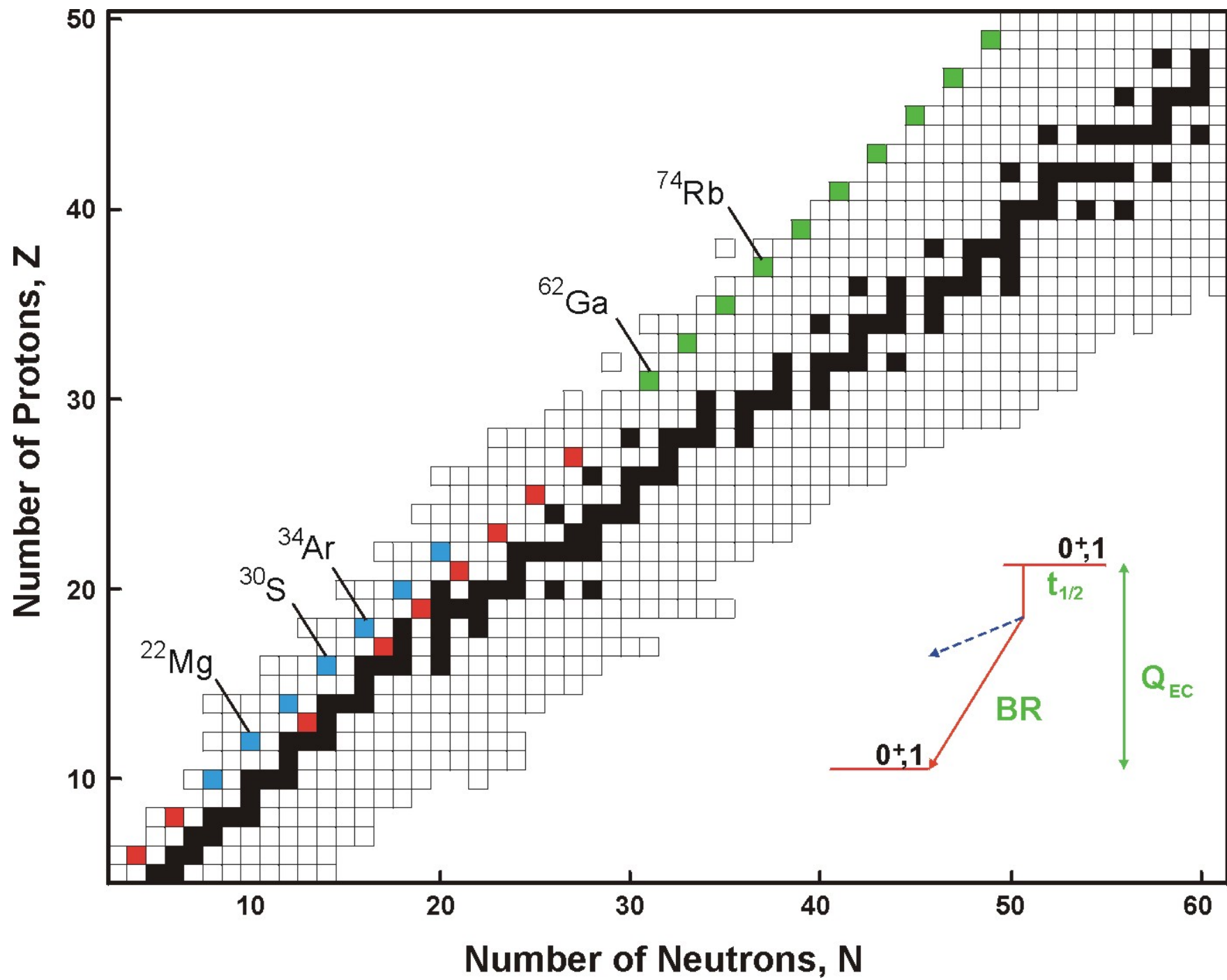
from: N. Severijns, M. Beck, O. Naviliat-Cuncic,
Rev. Mod. Phys. 78 (2006) 991



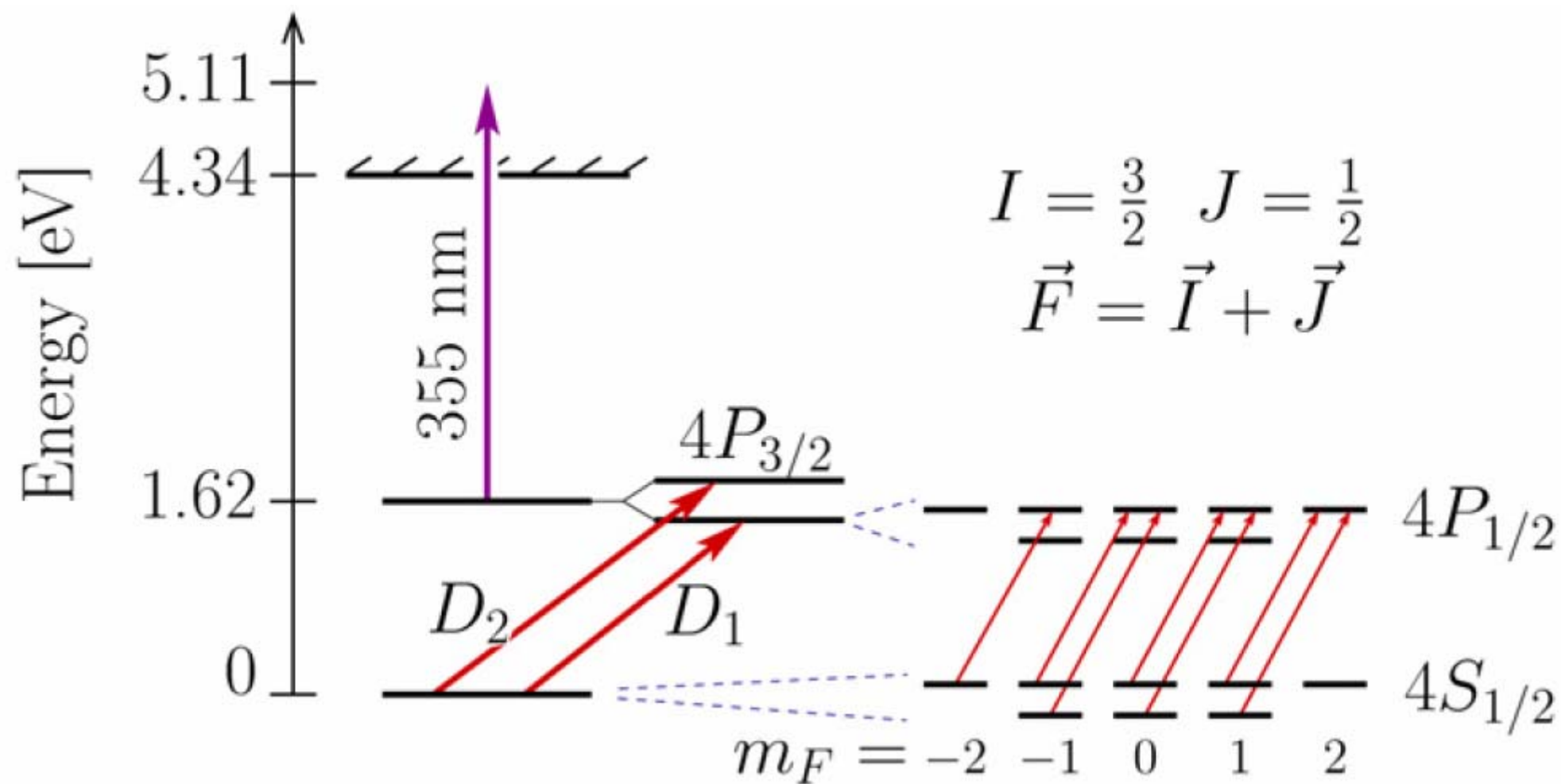
- * **no time reversal violation**
(apart from the small CP-violation described by the phase in the CKM matrix)

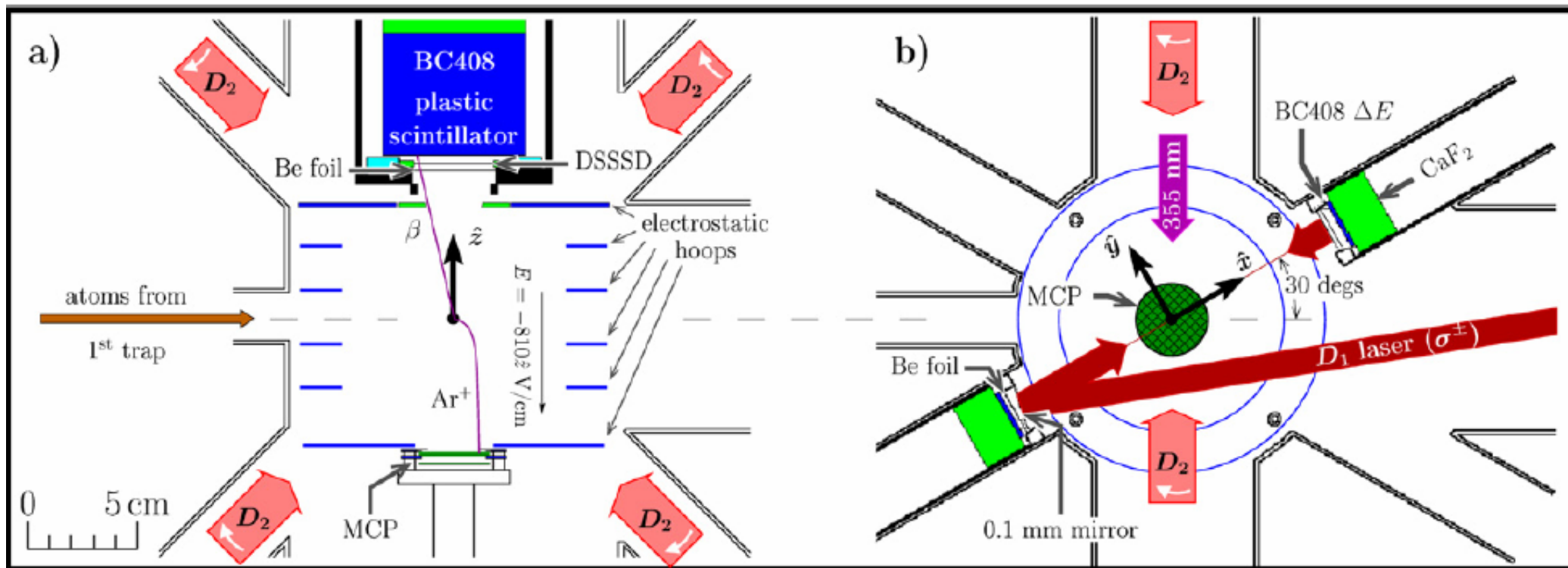
Comparison of beta decay rho results with collider results, assuming general LRS models





(J.C. Hardy)





Princeton D(^{19}Ne) experiment

- polarized ^{19}Ne from Stern-Gerlach magnet

- $\langle \vec{p}_e + \vec{p}_\nu + \vec{p}_R \rangle = 0$ for atoms in the cell $\rightarrow \vec{J} \cdot (\vec{p}_e \times \vec{p}_\nu)$ is equivalent to $-\vec{J} \cdot (\vec{p}_e \times \vec{p}_R)$

- $E(^{19}\text{F}^-) < 200 \text{ eV}$

result: $D = +0.0004(8)$

F. Calaprice et al., 1969 - 1984

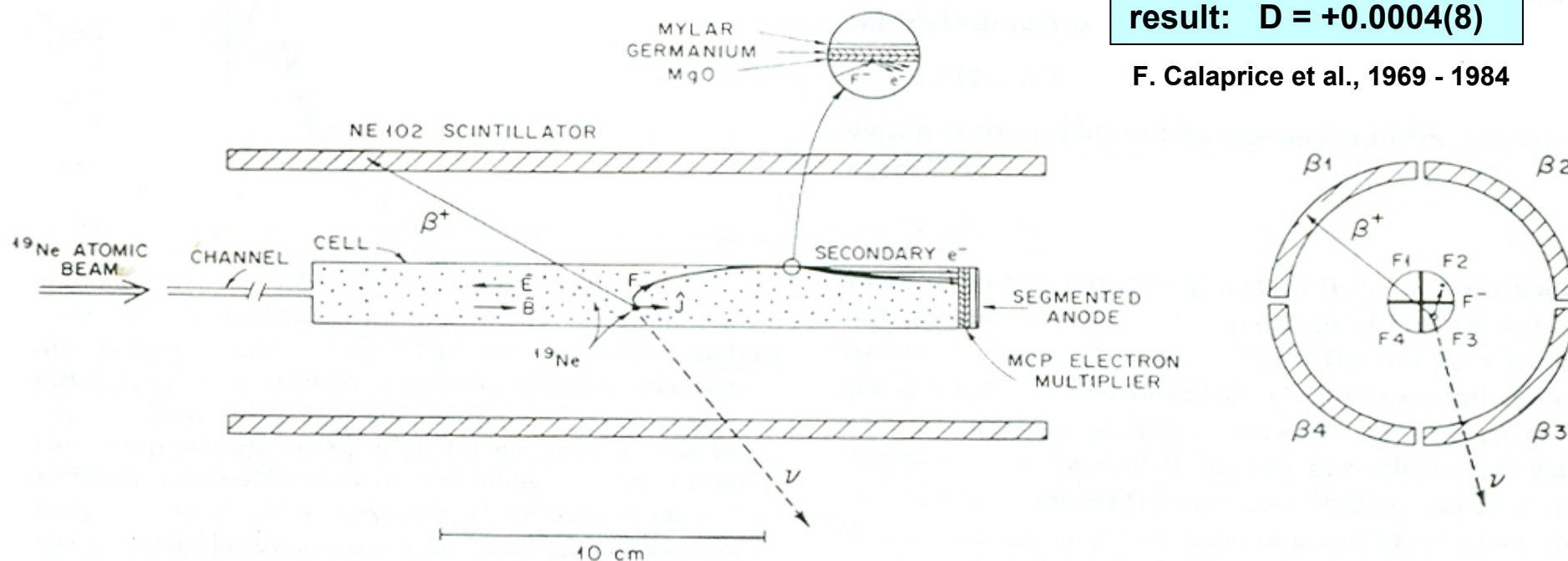
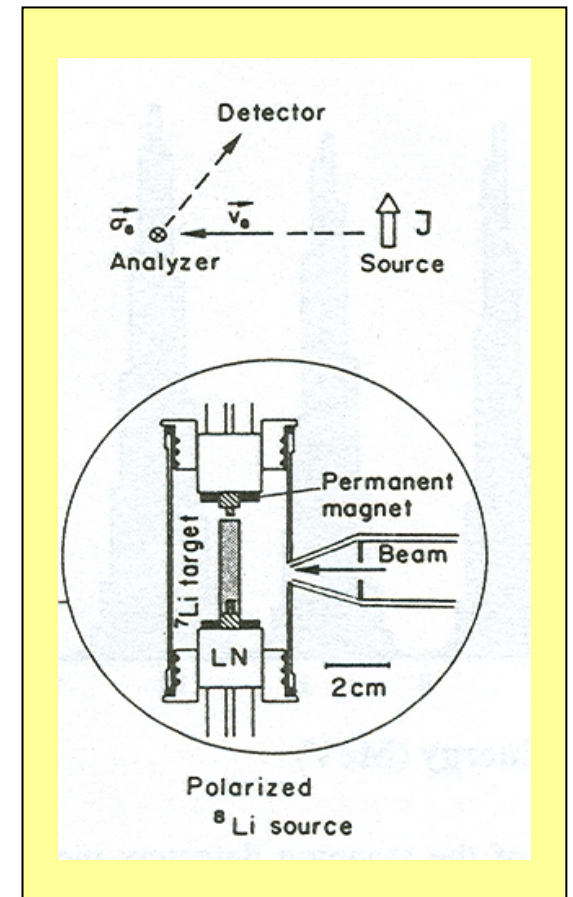
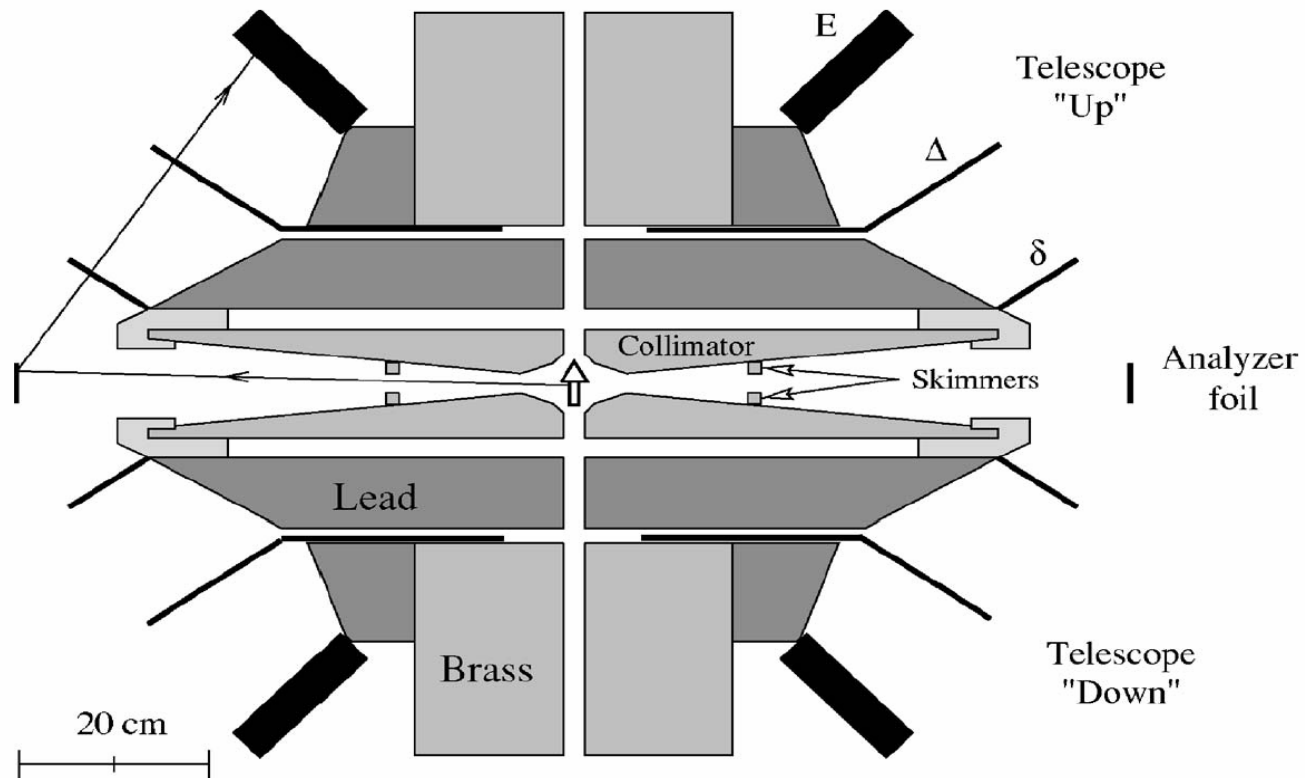


FIG. 1. Schematic illustration of the cylindrical cell and the detector system. Polarized ^{19}Ne , which enters the cell through a long narrow channel, fills the entire cell (dots). A uniform magnetic field maintains the polarization along the cell axis. In a typical decay the positron passes through the thin wall of the cell to one of four plastic scintillators (β_1 through β_4). The F^- recoil ion is accelerated along the cell axis by an electric field. The ion strikes the inside surface emitting secondary electrons which are accelerated into an electron multiplier segmented in four parts (F_1 through F_4).

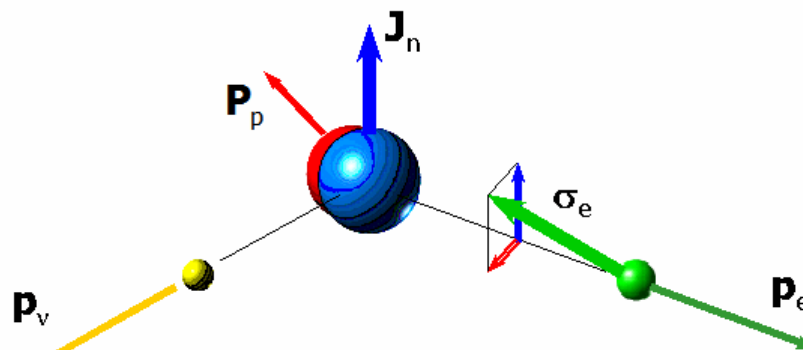
experimental set-up and result - ^8Li



3. Testing time reversal violation in free neutron decay

(Univ. Krakow, PSI, LPC-Caen, K.U.Leuven, ...)

(SINQ-FUNSPIN)

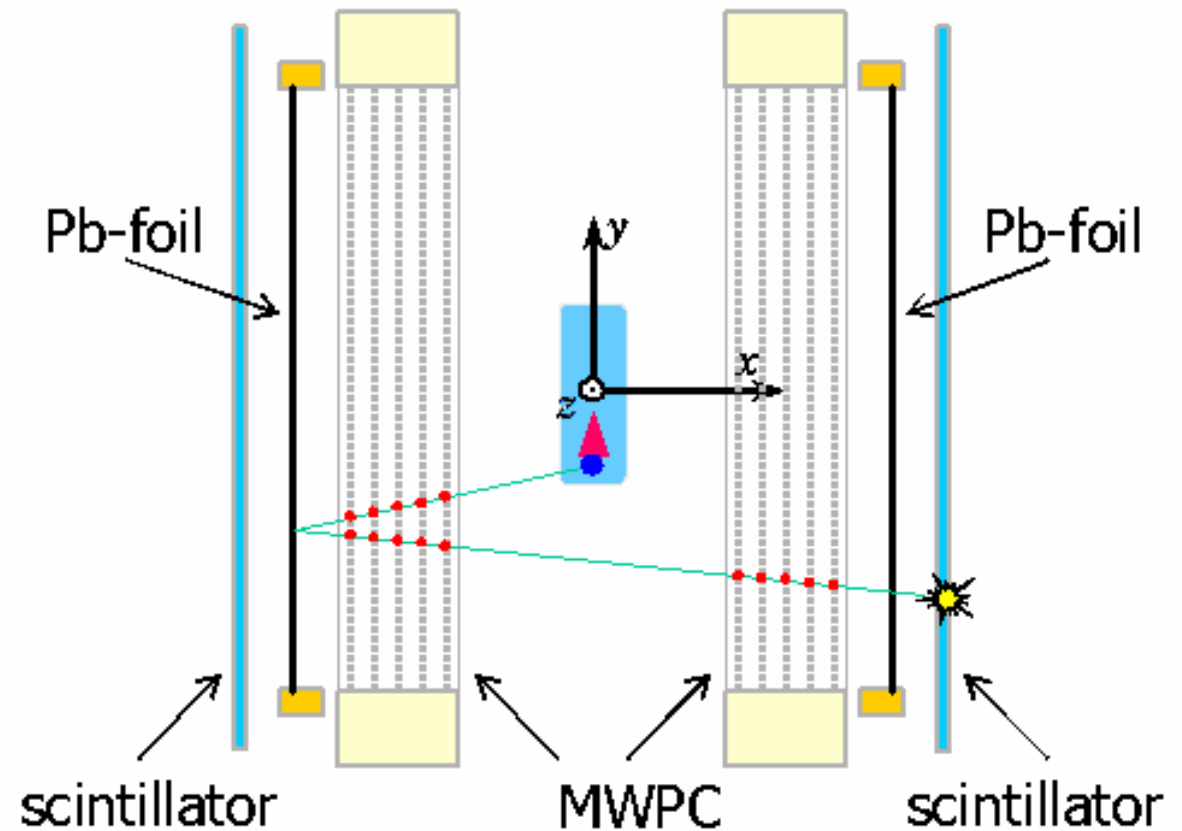


A diagram illustrating the kinematics of neutron decay. A central blue sphere represents the neutron, with a red arrow labeled \mathbf{p}_p (proton momentum) and a blue arrow labeled \mathbf{J}_n (neutron spin) originating from it. To the left, a yellow arrow labeled \mathbf{p}_ν (neutrino momentum) points away. To the right, a green arrow labeled \mathbf{p}_e (electron momentum) points away. A green arrow labeled σ_e (electron polarization) is shown near the electron. Above the diagram is the formula for the asymmetry parameter R :

$$R \frac{\vec{J} \cdot (\vec{p} \times \vec{\sigma})}{E}$$

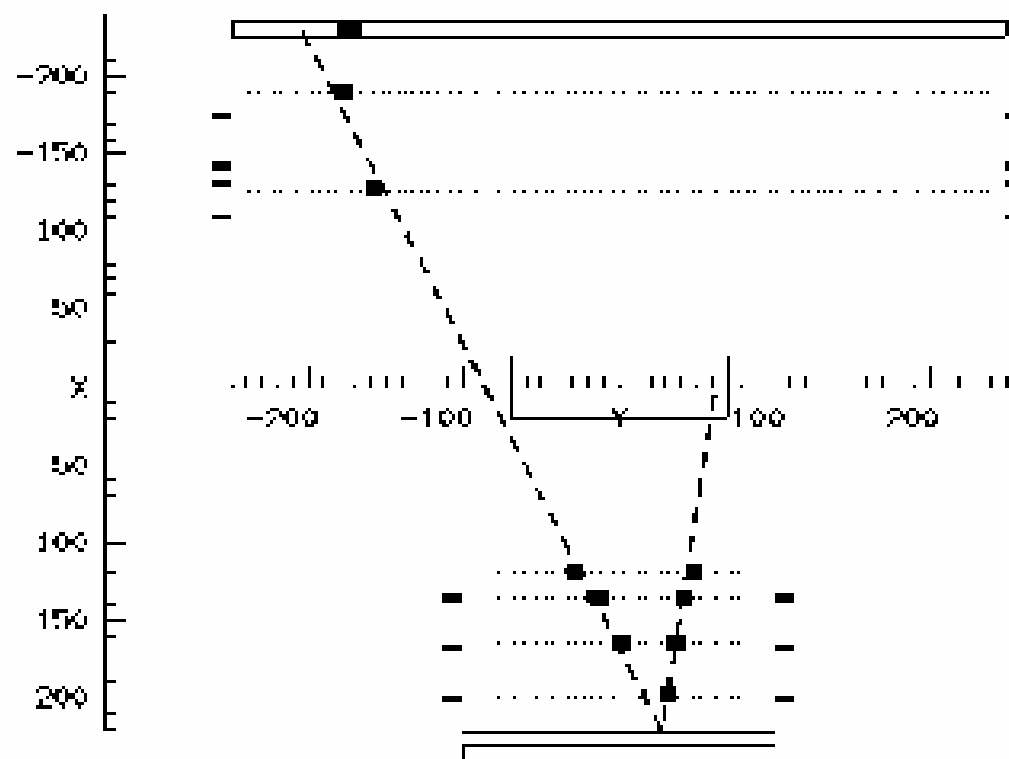
Below the diagram is the formula for the asymmetry parameter R in terms of coupling constants:

$$R = 0.28 \operatorname{Im} \left(\frac{C_S + C'_S}{C_A} \right) + 0.33 \operatorname{Im} \left(\frac{C_T + C'_T}{C_A} \right)$$



EVENT NO.: 38385 FTIF: ON ITNF

YX PROJECTION



ZX PROJECTION

